

Resource Allocation for Federated Learning in UAV-aided Digital Twin Edge Networks

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Giang Pham

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Introduction

Digital Twin (DT)

- **Intelligent** system, digitally **replicate** a physical object (PO)
- To **monitor, control, and optimize** POs during its life cycle

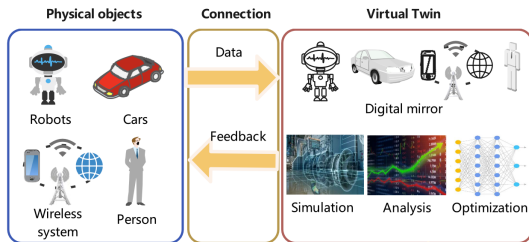


Figure 1: DT concept

TABLE 1. The three types concept of DT.

Concept	Functions	Physical-to-twin	Twin-to-physical
Monitoring DT	Virtual representation	×	×
Simulation DT	Simulation	✓	×
Operational DT	Co-evolute digital replica	✓	✓

Digital Twin Edge Networks (DITEN) - Where?

- DT are built, maintained by **mobile edge computing (MEC)**
- **Virtual twin-to-twin comms** construct a network DITEN
 - **Applications:** instruct POs from a **centralized** perspective
 - **Network:** optimize **directly** resource allocation, caching, ...

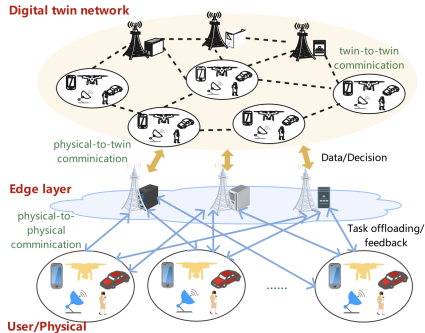


Figure 2: DITEN concept

Federated Learning (FL) - How?

- Centralized machine learning: frequent **data** exchange
 - High risk of **data leakage**
 - Synchronizing all raw data results in **over-comms load**
- Decentralized federated learning: **model parameters** exchange
 - **Protect user privacy**: devices locally train their ML model based on its own data
 - **Reduce comms load**: transmit only local model parameters

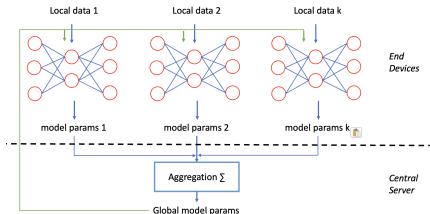


Figure 3: Federated learning

Problem: comms cost is **higher** than comp cost

System Model

UAV-aided DITENs for Internet of Vehicles

- K moving vehicles on the road, high density at the intersection
- A base station BS - MEC server integrated
- A UAV (fixed hovering at intersection): relay node, provides **higher prob.** of line-of-sight (LoS) propagation channels with **additional comms time** (UAV-BS)

Scenario: DT construction in UAV-aided DITENs for IoV

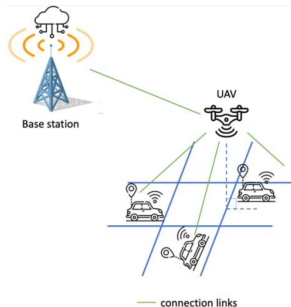


Figure 4: UAV-aided DITEN for vehicles

Federated Learning for DT construction

- DT construction time: τ
- Global accuracy: ϵ_0
- Local accuracy: η

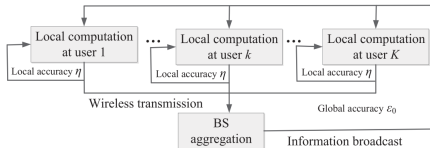


Figure 5: FL between vehs and BS

→ derive the **number of local rounds (i)** to reach the local accuracy η and the **number of global rounds (n)** to reach the global accuracy ϵ_0 **within** the DT construction time τ

Other key-points:

- Convex loss function → global convergence
- Non-convex loss function (?)

Problem Formulation

Optimization problem

Objective: **minimizing** the total energy consumption

Constraint: **guarantee** the DT construction time

	Energy	Time	Penalty
Comp	$e_k^{cp} = i \times \kappa C_k D_k f_k^2$	$t_k^{cp} = i \times \frac{C_k D_k}{f_k}$	
Comms	$e_k^{co} = n \times p_k t_k^{co}$	$t_k^{co} = n \times \frac{s_k \ln(2)}{B \ln(1 + \frac{p_k h_k}{N_0})}$	0, δ_t

- $i = v * \log_2(\frac{1}{\eta})$, $n = \frac{a}{1-\eta}$
(v, a : constants, depend on loss function, data)
- δ_t : penalty time *if* choosing UAV
- Optimization variables: η, f_k, p_k, x_k
 $x_k = 1$ *if* choosing UAV *else* 0

Problem formulation

$$\begin{aligned} \min_{\eta, f_k, x_k, p_k} \quad & \sum_{k=0}^{K-1} \frac{a}{1-\eta} \left(p_k \frac{s_k \ln(2)}{B \ln(1 + \frac{p_k h_k}{N_0})} + v \log_2 \left(\frac{1}{\eta} \right) \times \kappa C_k D_k f_k^2 \right) \\ \text{s.t.} \quad & \frac{a}{1-\eta} \left(\frac{s_k \ln(2)}{B \ln(1 + \frac{p_k h_k}{N_0})} + \Delta_k + v \log_2 \left(\frac{1}{\eta} \right) \times \frac{C_k D_k}{f_k} \right) \leq \tau, \\ & 0 \leq \eta \leq 1, \\ & 0 \leq f_k \leq f_k^{\max}, \forall k, \\ & x_k = \{0, 1\}, \forall k, \\ & 0 \leq p_k \leq p_k^{\max}, \forall k, \\ & h_k = (x_k == 1) ? h_k^{uav} : h_k^{bs}, \\ & \Delta_k = (x_k == 1) ? \delta_t : 0 \end{aligned}$$

Network Optimization

- **Interactive** bw FL and network optimization
- **Iterative** procedure
 - η : (fixed f_k, x_k, p_k): (convex) bound tightening by solving Lambert-W functions of constraints \Rightarrow Dinkelbach method for fractional form optimization
 - f_k, p_k : (fixed η): (convex) - solving 1st derivative $\nabla f = 0$, but **complex to generate closed-form solution** \rightarrow iterative algorithms (Newton's method, ...) to derived the solutions
 - x_k : heuristic to choose the better choice (method depends on the above iterative algorithm cost)

Simulation

Simulation scenario

- Dataset (for train, test): **represent** the vehicle's data
 - Synthetic: computer generated
 - MNIST: handwritten images, 10 output classes
 - FeMNIST: Federated Extended MNIST: handwritten images + others, 62 output classes
- Loss function (convex):
 - Linear regression: Regression problem
 - Multinomial logistic regression: Classification problem
- Modeling moving vehicles

Initial results - Synthetic

Synthetic dataset

- Input dim: 3, output dim: 5
- Loss: Linear regression
- Local rounds $i = 30$

Result:

- Loss, Acc converge after 50 global rounds
- Dissimilarity (square root of difference bw global gradient and local gradients) is small (small dataset)

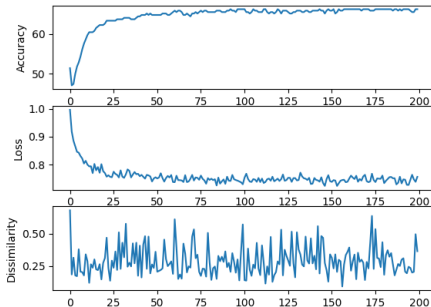


Figure 6: FL loss and accuracy - Synthetic

Initial results - MNIST

MNIST Dataset

- 28×28 images, input dim: 784, output dim: 10
- Loss: Multinomial logistic
- Local rounds $i = 30$

Result:

- Loss, Acc converge after 60 global rounds

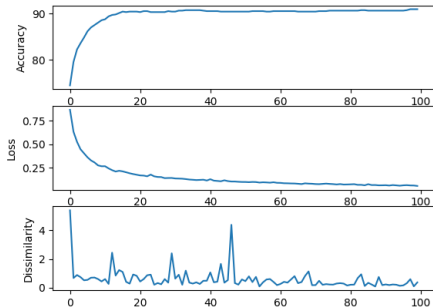


Figure 7: FL loss and accuracy - Synthetic

References

- [1] F. Tang, X. Chen, T. K. Rodrigues, M. Zhao and N. Kato, "Survey on Digital Twin Edge Networks (DITEN) Toward 6G," in IEEE Open Journal of the Communications Society, vol. 3, pp. 1360-1381, 2022, doi: 10.1109/OJCOMS.2022.3197811.
- [2] Z. Yang, M. Chen, W. Saad, C. S. Hong and M. Shikh-Bahaei, "Energy Efficient Federated Learning Over Wireless Communication Networks," in IEEE Transactions on Wireless Communications, vol. 20, no. 3, pp. 1935-1949, March 2021, doi: 10.1109/TWC.2020.3037554.

Thank you for your attention.