

Throughput Analysis of Incremental Redundancy Hybrid ARQ for FSO-based Satellite Systems

Hoang D. Le¹, Vuong V. Mai², Chuyen T. Nguyen³, and Anh T. Pham¹

¹Computer and Communications Lab., The University of Aizu, Japan

²Photonics Systems Research Laboratory, KAIST, Korea

³School of Electronics and Telecommunications, Hanoi University of Science and Technology, Vietnam

Hawaii-USA, Sept. 25, 2019



Outline

○ Introduction

- Free Space Optical (FSO)-based Satellite Systems
- Challenges in FSO-based Satellite Systems
- Solutions and Motivation

○ System Proposals

- IR-HARQ and Burst Transmission Design
- Channel-state Modeling
- Burst Loss Model
- Throughput Analysis

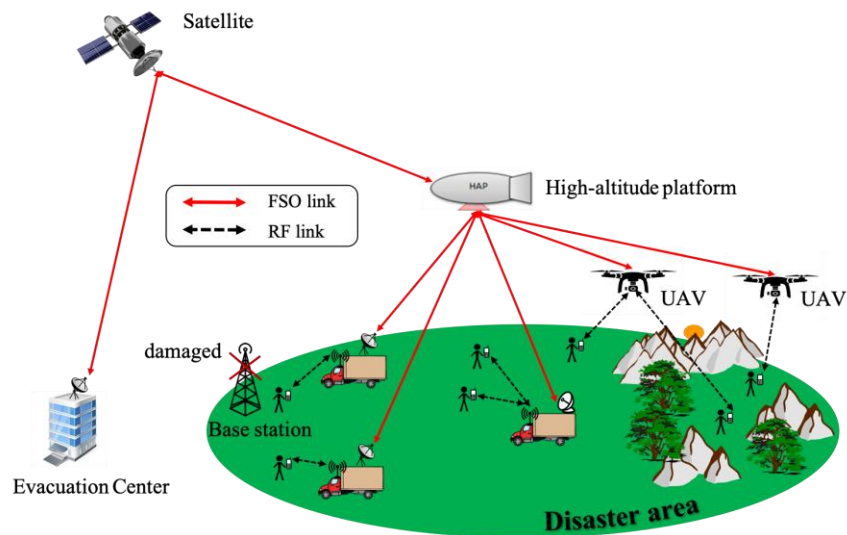
○ Numerical Results

○ Conclusions

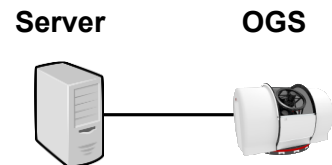
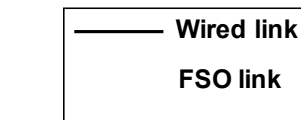
Free Space Optical (FSO)-based Satellite

○ FSO-based satellite communications:

- Availability of vast unlicensed bandwidth (using laser to provide ~ Gbps of data rate)
- Flexible deployment and wide coverage area (could be deployed for rural and remote areas)



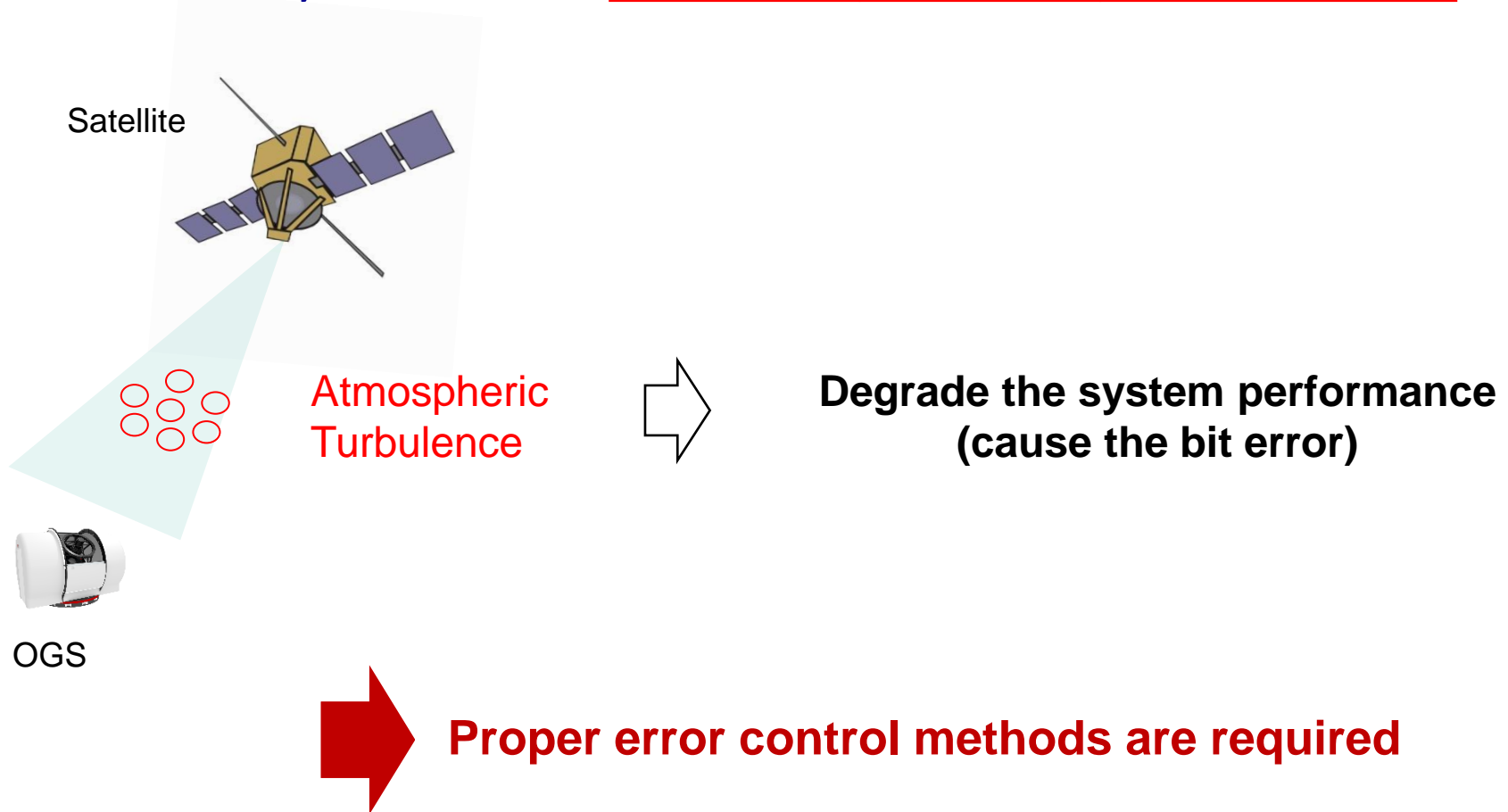
(1) Disaster recovery



(2) Internet-based access

Challenge in FSO-based Satellite System

- One of the main challenging issues in the design of FSO-based satellite systems is the uncertainty of atmospheric channels



Error Control Solutions

- Automatic repeat request (ARQ) and forward error correction (FEC) are the most popular error-control protocols [1]-[2].

[1]. DLR group, "Channel Modelling for Free-Space Optical Inter-HAP Links Using Adaptive ARQ Transmission," SPIE 2014

[2]. Eiji Okamoto, et al., "A Markov-Based Satellite-to-Ground Optical Channel Model and Its Effective Coding Scheme," IEICE Trans. Com., 2012

- For FSO-based satellite:

- ARQ may **not efficient** in high-latency networks when channel becomes noisy (requires many retransmissions)
- FEC always **requires redundancy** and may **reduce system throughput** (more redundancy, more reliable, but reduce throughput)

→ **The solution (combine FEC and ARQ): retransmit only redundancy for erroneous frame and combine with previous received ones to correct that frame**



**Incremental redundancy hybrid ARQ (IR-HARQ) protocol
which has not been investigated for FSO-based satellite systems**

What's Our Goal?

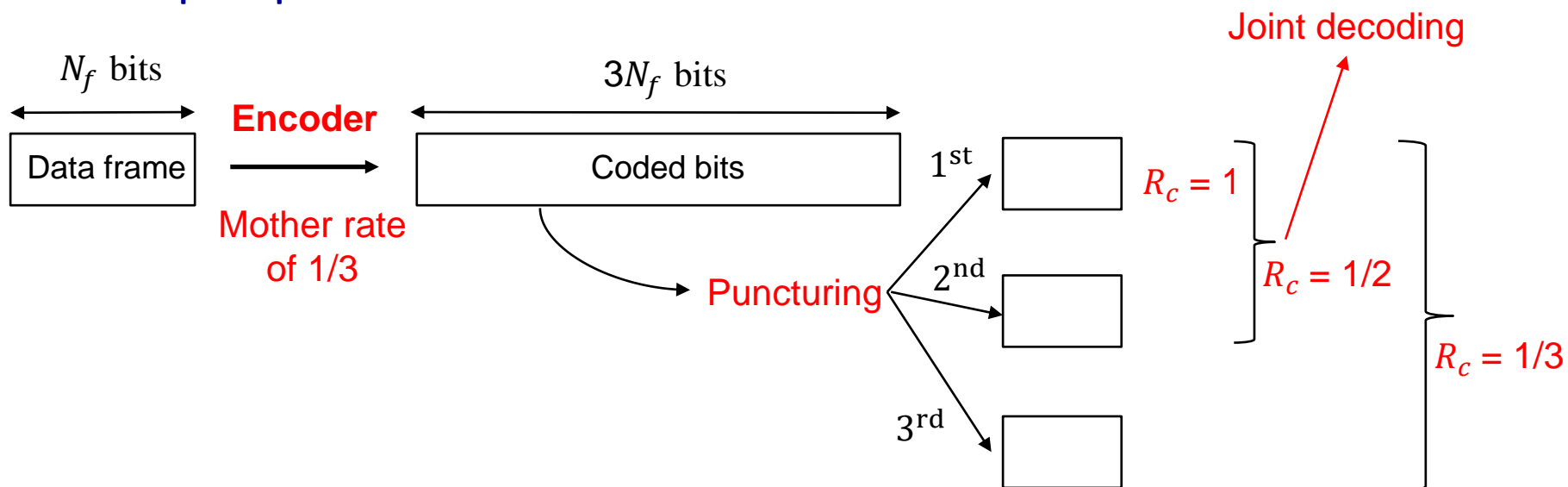
- We want to see how IR-HARQ can be applied for FSO-based satellite communication systems
 - Uncertainty of atmospheric channels
 - High-latency of satellite systems
 - High speed connection: different from RF communications
- Our goals:
 - We study the **design of IR-HARQ protocol** for FSO burst transmission in satellite communication system
 - Find the **optimal setting** (provided turbulence conditions and connection speed) for **system performance** (throughput)

IR-HARQ Protocol

○ IR-HARQ protocol

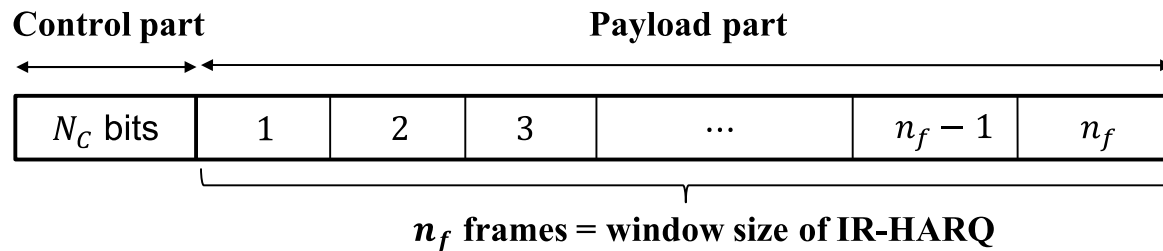
- Rate-compatible puncturing convolutional code (RCPC): a data frame encoded by a mother code (low code rate, e.g., 1/3), is punctured into the coded bits with higher code rates for transmissions
- Sliding window ARQ: using selective-repeat mechanism to retransmit the coded bits and combine all the previous received ones to correct the frame

○ Example: persistent level of HARQ = 3



Burst Transmission Design

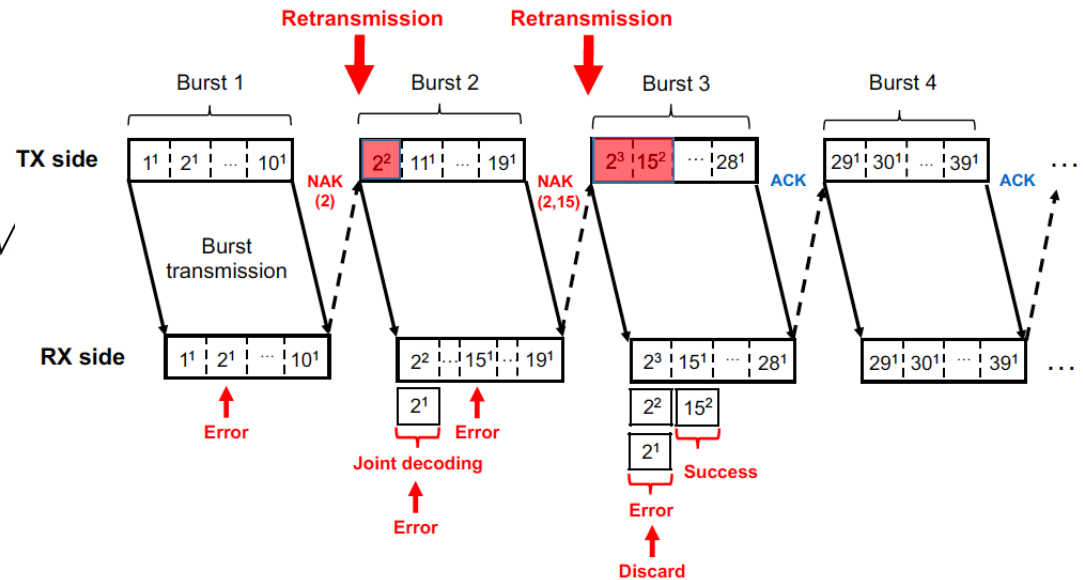
- Long channel coherence time → design the burst transmission at the PHY layer
 - Coherence time of FSO channels is typically 1 to 10ms or longer [3].
[3]. I. Djordjevic, "Adaptive modulation and coding for free-space optical channels," IEEE JOCN 2010
 - For example: 1Gbps FSO transmission takes **1 μ s** to transmit one frame with size of 1080 bits, and it may cover at least 1000 frames in a coherence time
- Burst transmission
 - Control part: for the detection of burst at receiver
 - Payload part: contains multiple frames deigned by a window size of IR-HARQ



Example of Burst Transmission

○ Example:

- Burst size = 10 frames
- Persistent level of IR-HARQ, $N = 3$



- To analyze system throughput, we need to build the burst loss model

- Consider the time-varying behavior of turbulence fading and channel modeling for burst transmission

- Gamma-gamma (GG) turbulence fading channel is assumed [3]

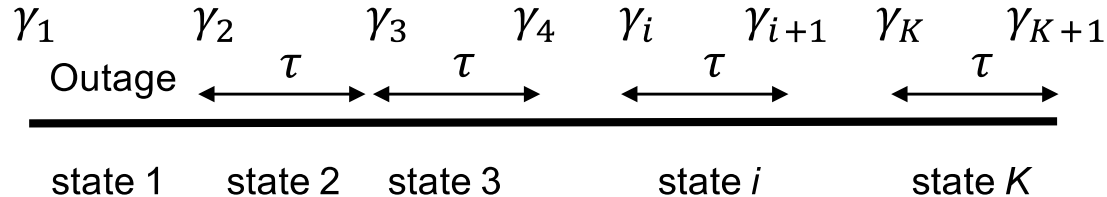
[4]. D. R. Kolev, et al., (NICT), "Received-Power Fluctuation Analysis for LEO Satellite-to-Ground Laser Links," IEEE JOCN 2017

Channel-State Modeling

- Modelling the burst transmission over turbulence fading channel

→ The transmission of burst and its feedback signal is assumed to be within a fixed-time slot of channel states whose average duration is chosen to be shorter than the fading coherence time

γ : signal-to-noise ratio (SNR) threshold



Channel duration Probability of the channel state i -th

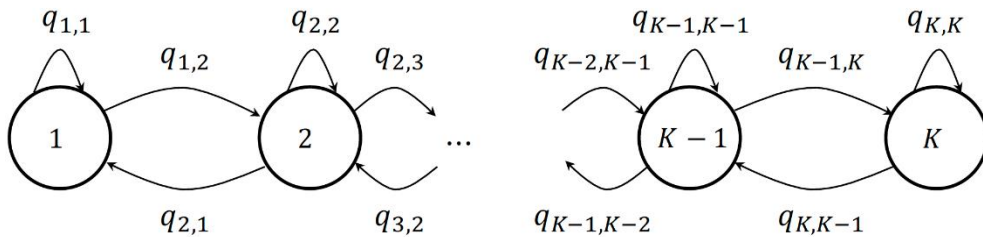
$$\bar{\tau}_i = \frac{\text{Pr}_i}{N(\gamma_i) + N(\gamma_{i+1})} = T_{\text{burst}} + 2t_{\text{prop}} \leq t_0$$

Level crossing rate at a given γ_i

Channel coherence time

Channel-State Transition

- Finite-state Markov Chain to model the behavior of channel



$q_{i,j}$: transition probability from i -th state to j -th state

Given $q_{i,j}$, we can find the steady-state probability, \Pr_i , at i -th state

$$q_{i,j} = \begin{cases} 0 & \text{if } |i-j| \geq 2, \\ \frac{N(\gamma_{i+1})T_{\text{burst}}}{\Pr_i} & \text{if } j = i+1 \text{ and } i = 1, \dots, K-1, \\ \frac{N(\gamma_i)T_{\text{burst}}}{\Pr_i} & \text{if } j = i-1 \text{ and } i = 2, \dots, K, \\ 1 - p_{i,i+1} - p_{i,i-1} & \text{if } i = j \text{ and } 0 < i < K, \\ 1 - p_{0,1} & \text{if } i = j = 0, \\ 1 - p_{K,K-1} & \text{if } i = j = K. \end{cases}$$



We use the channel model to develop the burst loss model for analyzing the system throughput

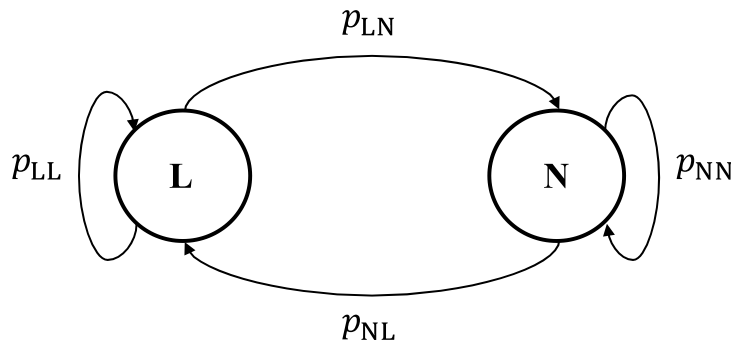
Burst Loss Model

- We develop the data burst loss model to derive the system throughput

- Loss state (L-state): burst loss happens (i.e., either the header is corrupted or one of frames is lost) with a probability,

$$\text{BLP}_i = 1 - (1 - \overline{\text{BER}}_{\text{H},i})^{N_c} \times (1 - \overline{\text{FLR}}_i)^{n_f}$$

- $\overline{\text{BER}}_{\text{H},i}$: average bit error rate of the control part at channel-state i -th
- $\overline{\text{FLR}}_i$: average frame loss rate at channel-state i -th
- Non-loss state (N-state): none of frames in burst are lost



- Transition probabilities

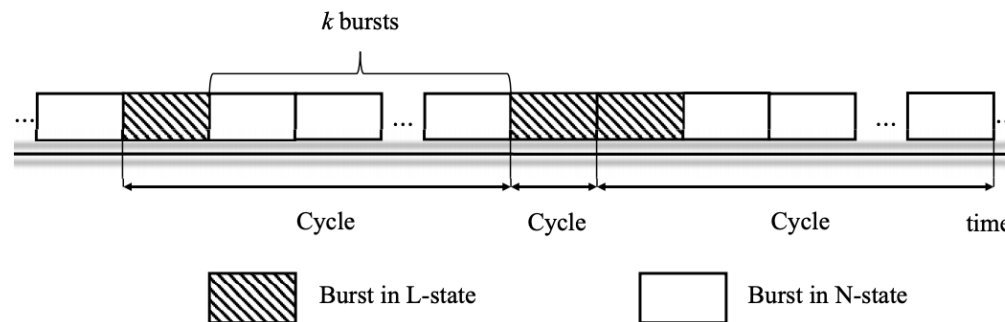
- $$p_{\text{LN}} = \frac{\sum_{i=1}^K \sum_{j=1}^K \text{Pr}_i \text{BLP}_i q_{i,j} (1 - \text{BLP}_j)}{\sum_{i=1}^K \text{Pr}_i \text{BLP}_i}$$

- $$p_{\text{NL}} = \frac{\sum_{i=1}^K \sum_{j=1}^K \text{Pr}_i (1 - \text{BLP}_i) q_{i,j} \text{BLP}_j}{\sum_{i=1}^K \text{Pr}_i (1 - \text{BLP}_i)}$$

- Pr_i : the steady-state probability at channel-state i -th
- q_{ij} : the transition probability from i -th to j -th channel-state

System Throughput Analysis (1)

- We consider an infinite sequence of transmitting bursts which is divided into cycles
 - Each cycle starts by a burst in L-state and ended by the burst just before another L-state one



- Throughput is defined as the **ratio** between the **average no. of successful received frames in a cycle** and **average cycle duration**

System Throughput Analysis (2)

○ System Throughput:
$$\bar{\eta} = \frac{E_f \times N_f}{(1 + E_b) \times T_{\text{slot}}}$$

- E_b : average no. of bursts in N-state of a cycle

$$E_b = p_{L,N} \times \sum_{k=1}^{\infty} k \times p_{N,L}(k) + 0 \times p_{L,L}$$

- E_f : average no. of successful frames in a cycle

$$E_f = \frac{E_b \times n_f}{\bar{M}} + \sum_{i=1}^{n_f-1} i \binom{n_f-1}{i} p_s^i (1-p_s)^{n_f-1-i} (1 - \overline{\text{BER}}_H)^{N_C}$$

- p_s : probability that a frame is correctable (received successfully)
- \bar{M} : average number of transmissions for a frame

Numerical Results

- We consider a FSO transmission from low-earth orbit (LEO) satellite to ground station
- The system parameters

Name	Value
Frame size	$N_f = 1500$ bytes
Burst-control part size	$N_C = 40$ bits
Persistent level of HARQ	$M = 3$
Data rate	$R_b = 1$ Gbps
Satellite Altitude	$H = 610$ km
Zenith angle	$\xi = 60^\circ$
Wind speed	$v_{\text{wind}} = 21$ m/s
RCPC family code	(1, 4/5, 1/2) (1, 1/2, 1/3)
Optical wavelength	$\lambda = 1.55$ μm

Burst Size Selections

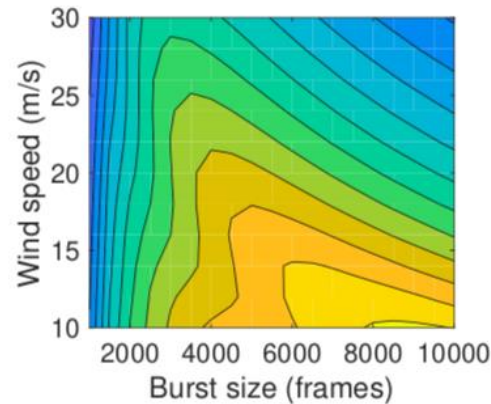
➤ $T_{\text{slot}} = T_{\text{burst}} + 2t_{\text{prop}} \leq t_o$

➤ Coherence time

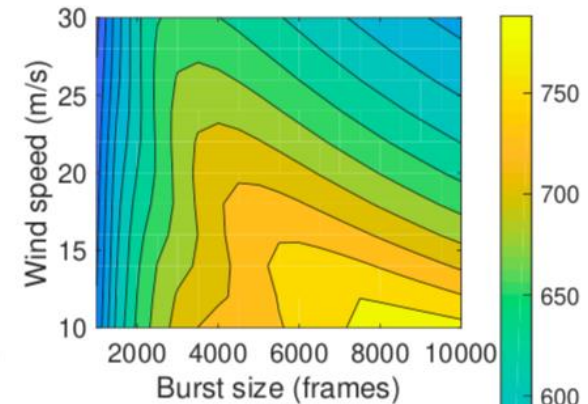
$$t_o = \frac{\sqrt{\lambda H \sec(\xi)}}{v_{\text{wind}}}$$



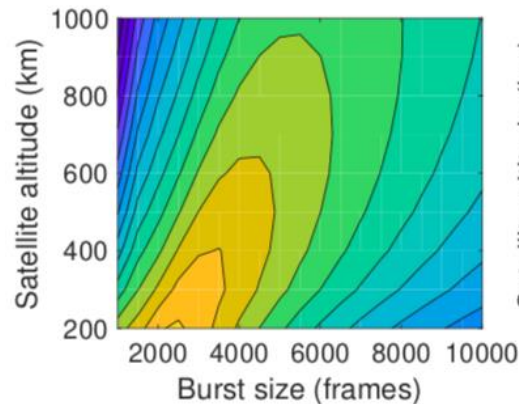
➤ By varying wind speed or satellite altitude, the optimal burst size can be observed to maximize system throughput



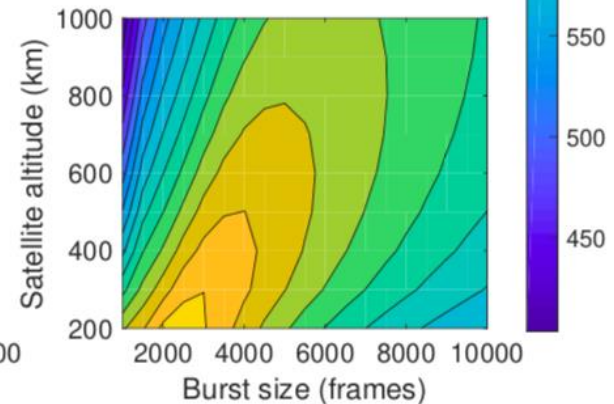
(a)



(b)



(c)

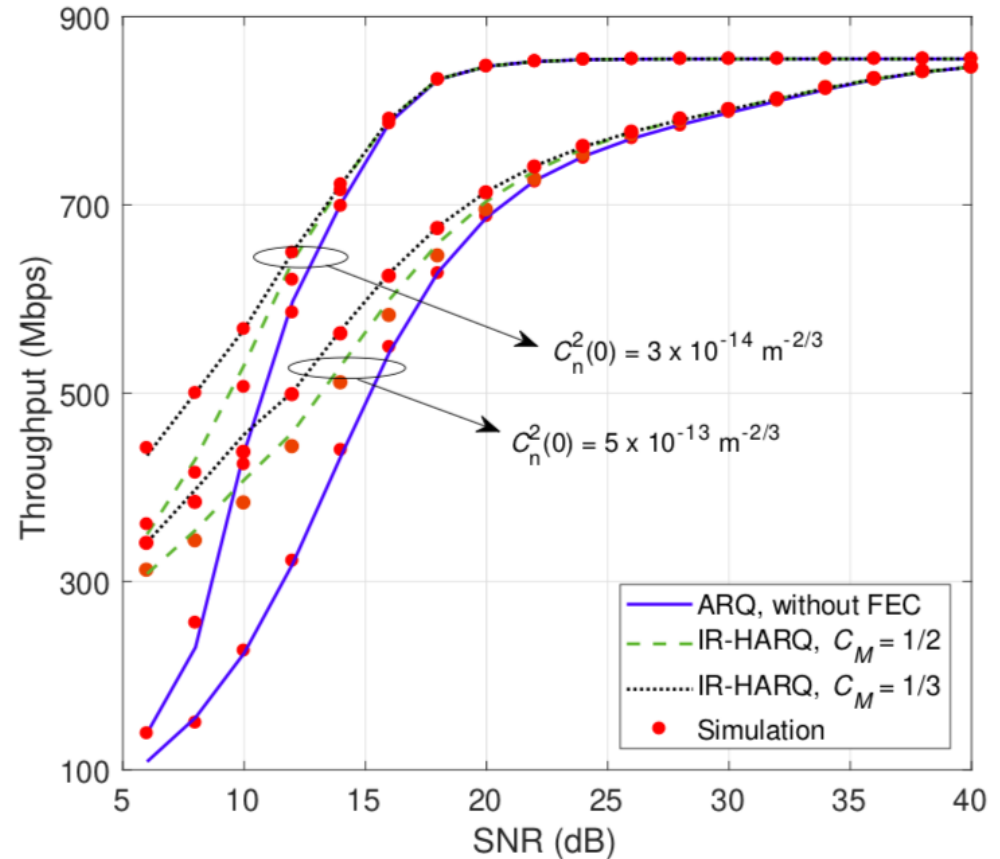


(d)

- Given $H = 610$ km: (a) $C_M = 1/2$ and (b) $C_M = 1/3$
- Given $v_{\text{wind}} = 21$ m/s: (a) $C_M = 1/2$ and (b) $C_M = 1/3$

Throughput vs. received SNR

- IR-HARQ outperforms pure sliding window ARQ in high error rate environment



Burst size = 4000 frames, $H = 610$ km, $v_{\text{wind}} = 21$ m/s

Conclusions

- The paper studied the design and analyzed the throughput performance of IR-HARQ protocol for FSO burst transmission in satellite communication systems.
- **Numerical results**
 - showed the impact of atmospheric turbulence on throughput performance.
 - confirmed the effectiveness of using IR-HARQ.
 - supported the optimal selection of burst size to maximize the system throughput.
- **Future work**
 - Consider a comprehensive design by exploring the queuing model and adaptive modulation and coding (AMC) schemes.

Thank you for your listening!

(Attendance supported by Telecommunications Advancement Foundation)



公益財団法人

電気通信普及財団

The Telecommunications Advancement Foundation