

*Fall 2015-Performance Evaluation of Network
Systems Course (CNA04)*

TCP and Modeling TCP Performance: A Review & Survey

Vuong Viet Mai
Computer Communications Lab.
1:30pm-3:00pm
November 24, 2015

Outline

1. Introduction

- TCP
- Performance Study of TCP/IP

2. TCP Congestion Control Review

- Congestion indications & reactions
- TCP variants classification

3. TCP Modeling

- *Renewal Theory Models*
- Fixed-point Methods
- Control Theoretic Models

4. Summary & Recommended Refs

Introduction: TCP

- *Transmission Control Protocol (TCP) is the predominant transport protocol used by IP technology to support popular Internet services*
- TCP applications & services
 - Most popular Internet applications use TCP
 - E-mail, WWW, file transfer, remote login, etc.

Introduction: TCP

- Motivation for Performance Study of TCP
 - Originally, TCP worked well in wired network
 - Nowadays, in heterogeneous networks: TCP algorithms & parameters that are suitable for one environment are not always suitable for other environments
 - Must acquire a solid foundation & understanding TCP performance through such networks

Introduction: Performance Study of TCP

- Tools & techniques

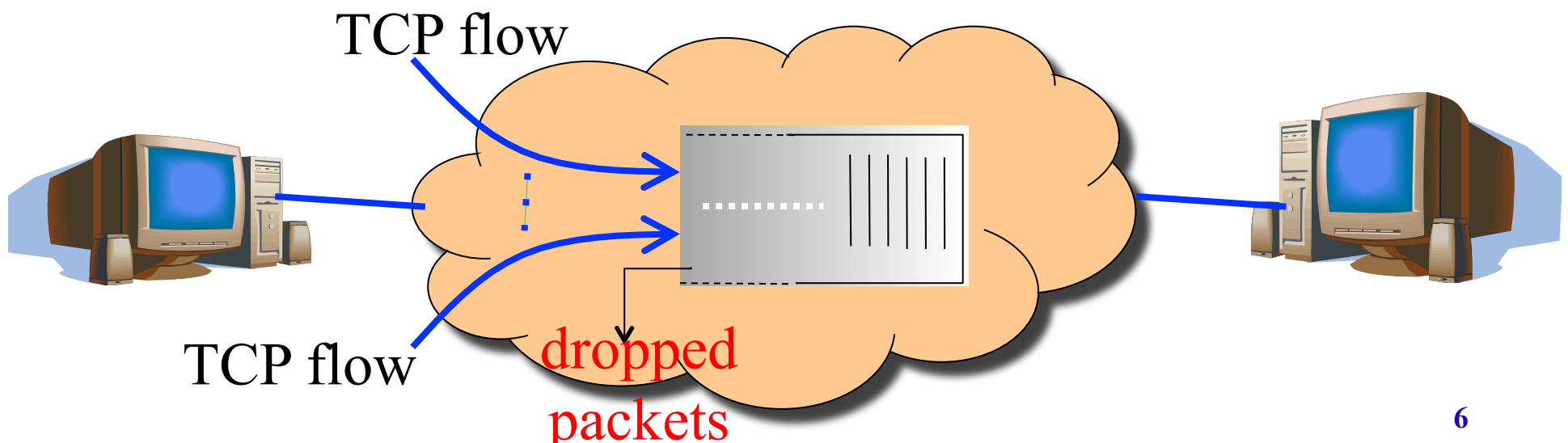
	Scopes
Measurement	<ul style="list-style-type: none">- Help users to reveal potential bottlenecks- Detect inadequate parameters settings- Test components reliability
Network simulation	<ul style="list-style-type: none">- Provides a convenient way to predict the performance when the proposed network is not available for measurement- Allows the evaluation of performance under a wide variety of workload & network- Can incorporate more details than analytical modeling; results can be produced that are closer to reality
Analytical modeling	<ul style="list-style-type: none">- <i>TCP connections operating across the Internet is a huge control system. We need mathematical models to capture a system of this magnitude</i>- <i>Convenience methods for design & optimization protocols</i>

Introduction: Performance Study of TCP

- Main focus of this lecture
 - TCP analytical modeling
 - Objectives
 - Gain an understanding of the basic TCP operations, focusing on “Congestion Control”
 - Understand the fundamental relationship between network parameters and TCP performance
 - Apply a range of “Mathematical Models” to predict TCP performance

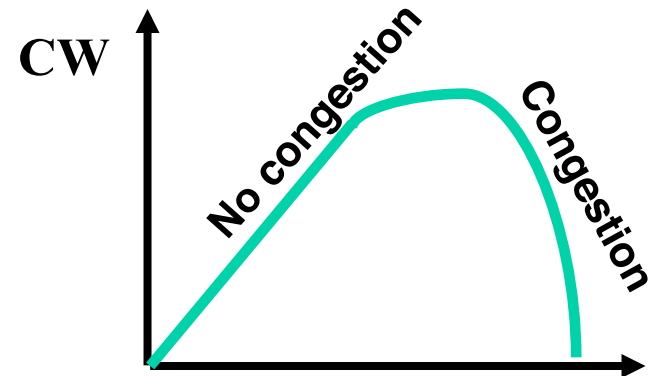
TCP Congestion Control Review

- What is congestion?
 - Load is higher than capacity
- What do IP routers do?
 - Drop the excess packets
- Why is this bad?
 - Wasted bandwidth for retransmissions; delay



TCP Congestion Control Review

- Congestion control
 - Keep senders from overloading the network
- Congestion window
 - Maximum data (bytes, packets) can be transmitted
- Upon *not detecting* congestion
 - *Increase* the window size
 - And see if the packets are successfully delivered
- Upon *detecting* congestion
 - *Decrease* the window size

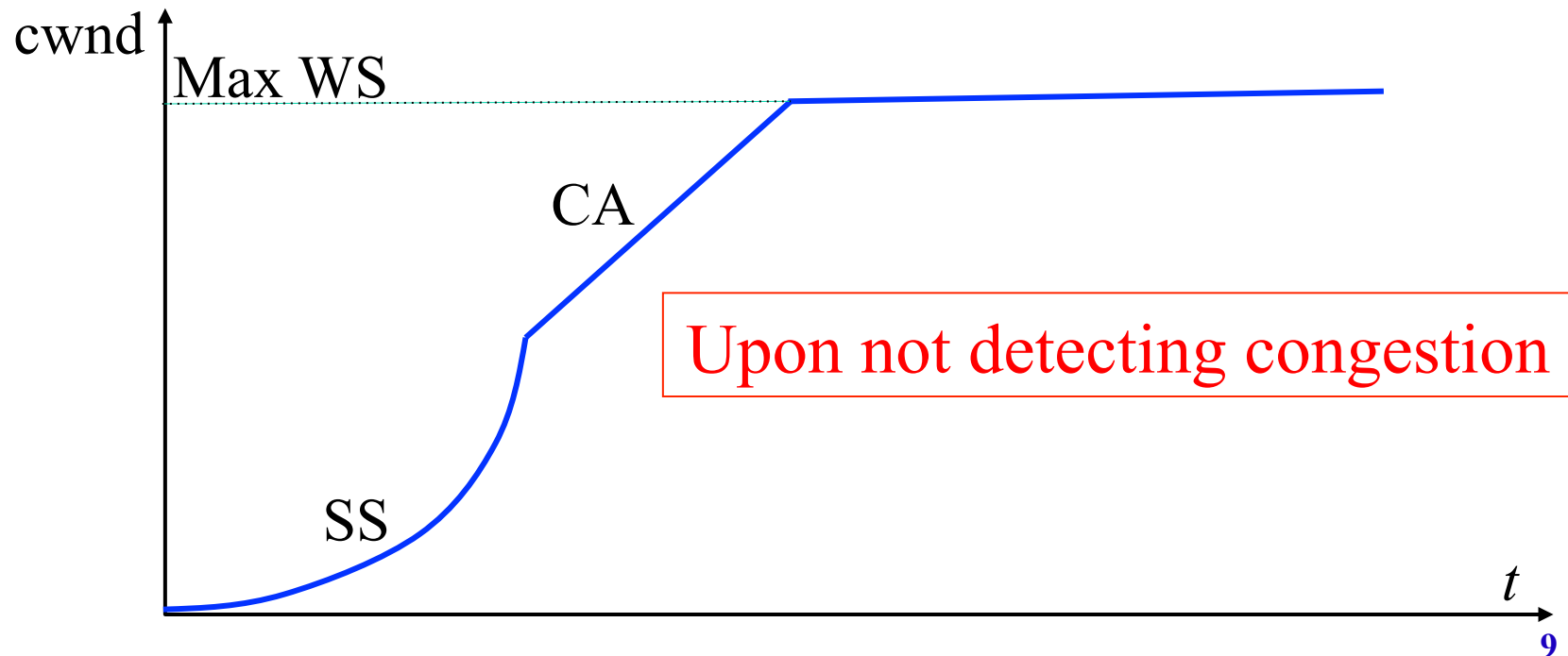


TCP Congestion Control Review

- Slow-start (SS) phase
 - Initially, CW is 1 Max Segment Size (MSS)
 - So, initial sending rate is MSS/RTT (slow rate)
 - Increases the rate exponentially
 - $cwnd = 2 * cwnd_{previous}$
 - Until cwnd reaches SS threshold (ssthresh)
 - Switch to the next phase

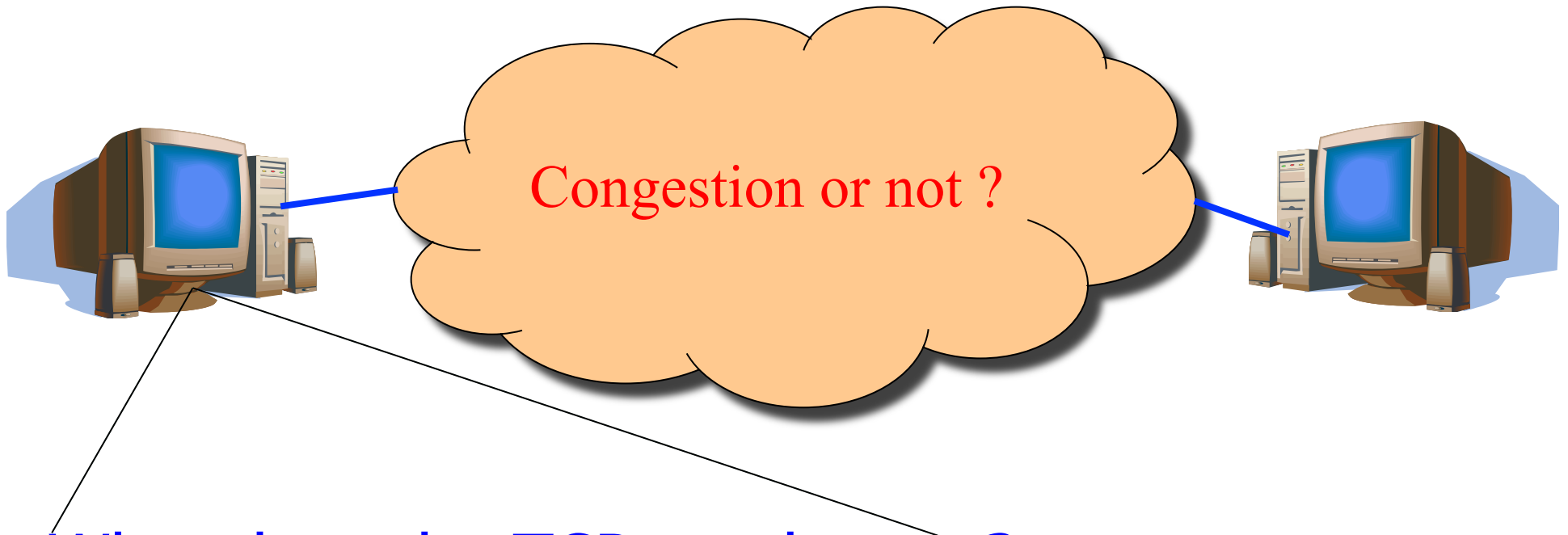
TCP Congestion Control Review

- Congestion Avoidance (CA) phase
 - Increases the rate linearly
 - $cwnd = 1 + cwnd_{previous}$
 - Until cwnd reaches Maximum CW
 - Keep CW constant



TCP Congestion Control Review

- Congestion indications



What does the TCP sender see?

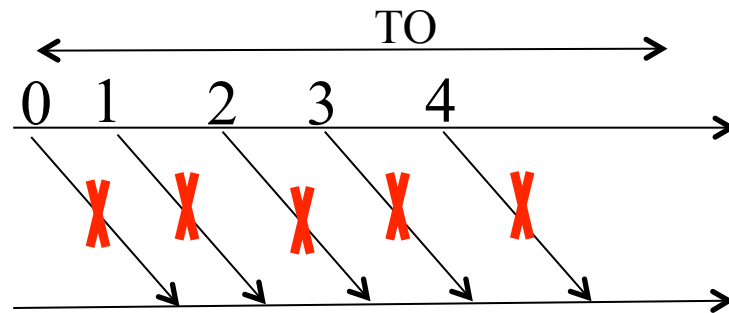
- Packet losses
- Round-trip delay

TCP Congestion Control Review

- Congestion indications

- Timeout

- Packet n is lost and detected via a timeout
 - E.g., because all packets in flight were lost
 - Serious congestion



TCP Congestion Control Review

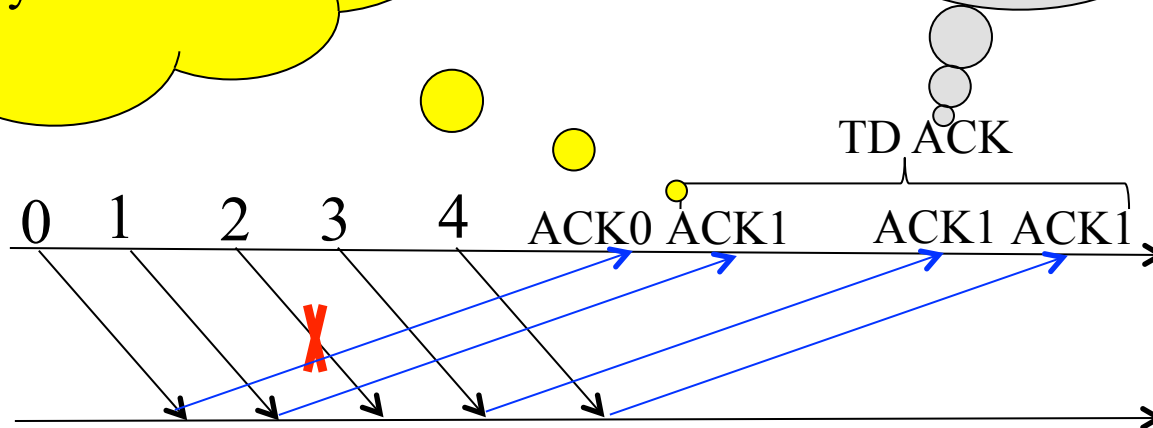
- Congestion indications

- Triple duplicate ACK

- Packet n is lost, but packets $n+1$, $n+2$, etc. arrive
 - Receiver sends duplicate acknowledgments
- Congestion but not serious

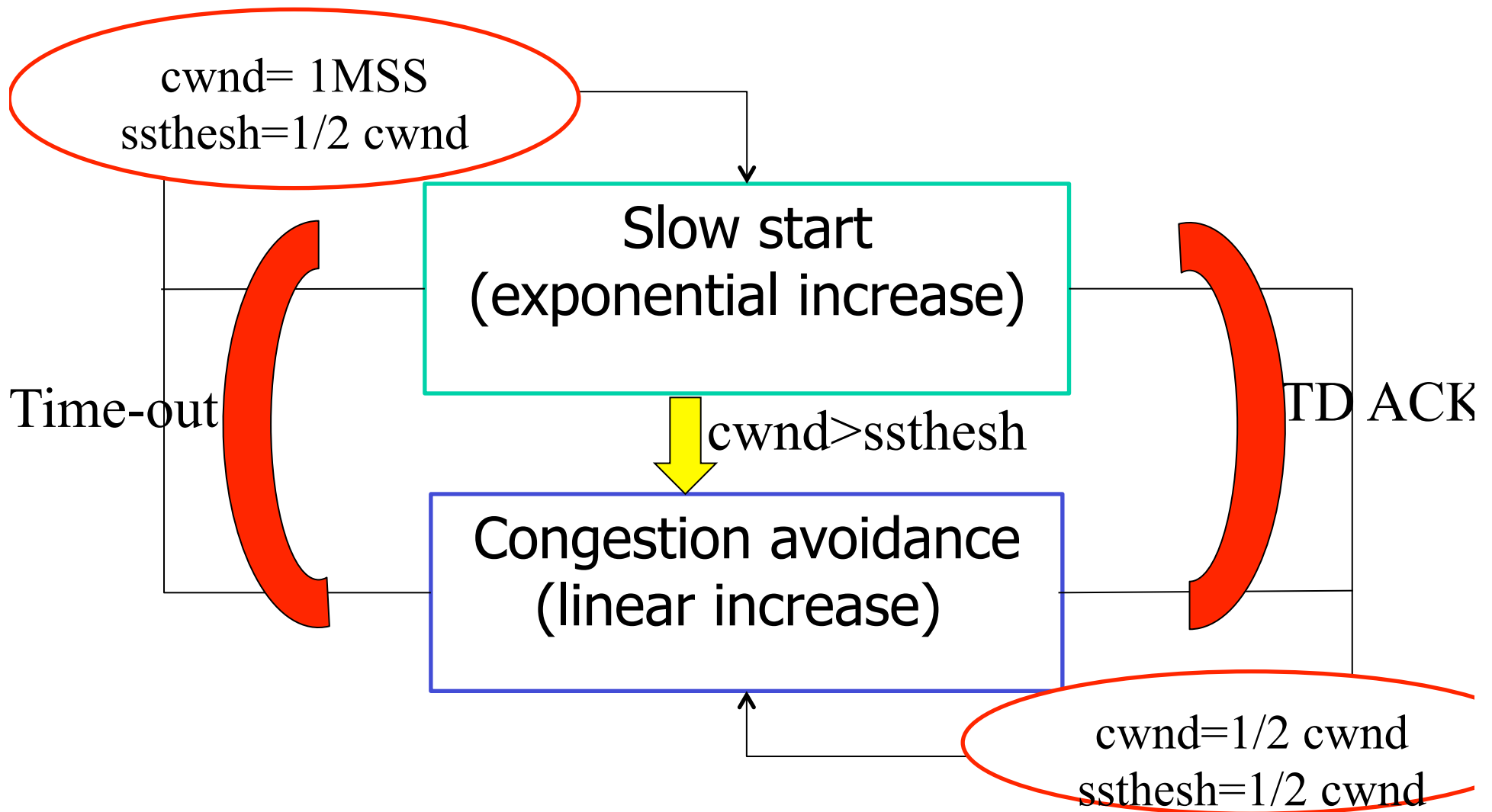
So far, all packets up to packet #1 have been safely received

Why “3”
-If “2”, too early
-If “4,...”, take long time



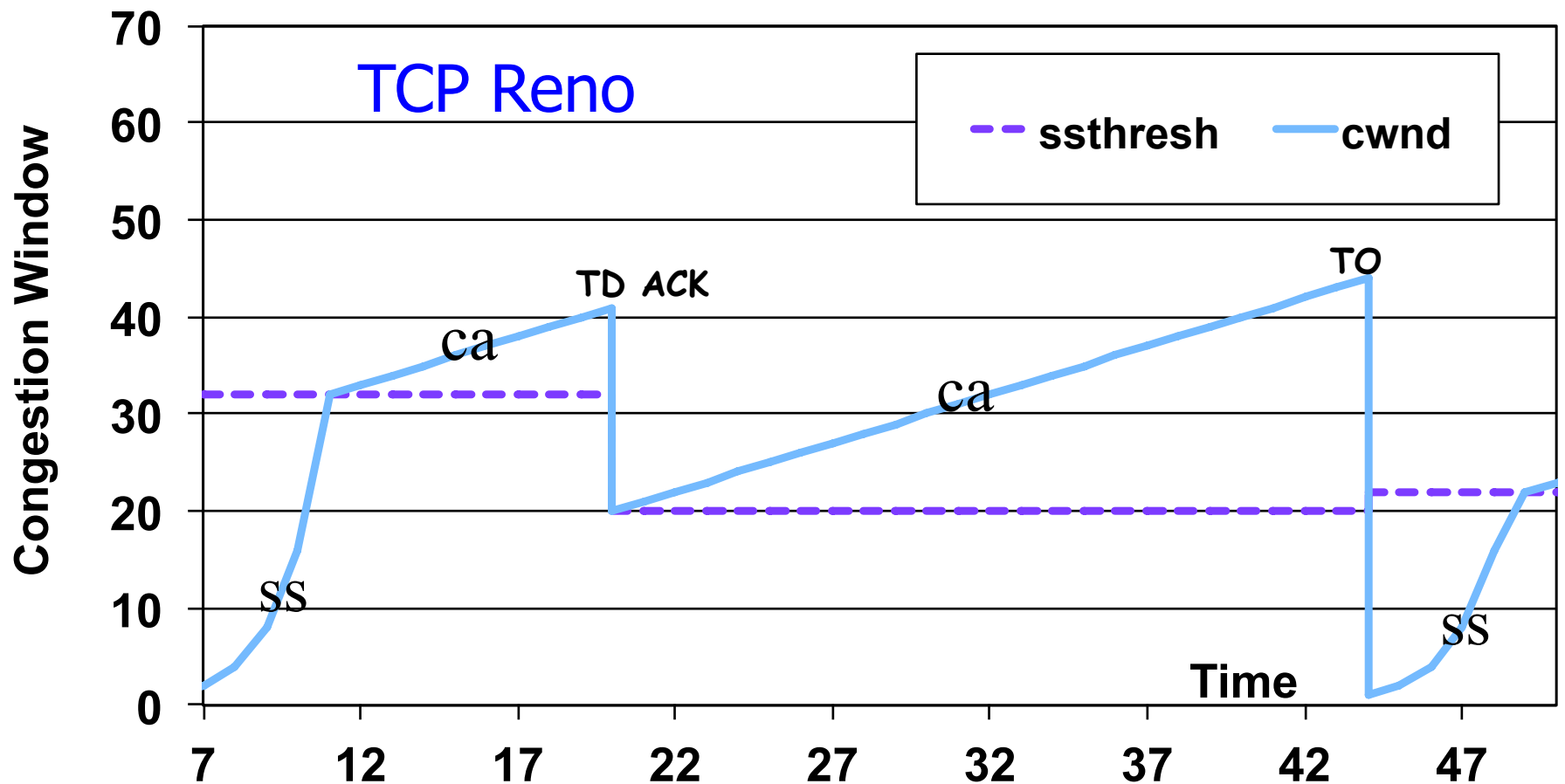
TCP Congestion Control Review

- Congestion reactions



TCP Congestion Control Review

- Congestion reactions
 - Congestion window trace



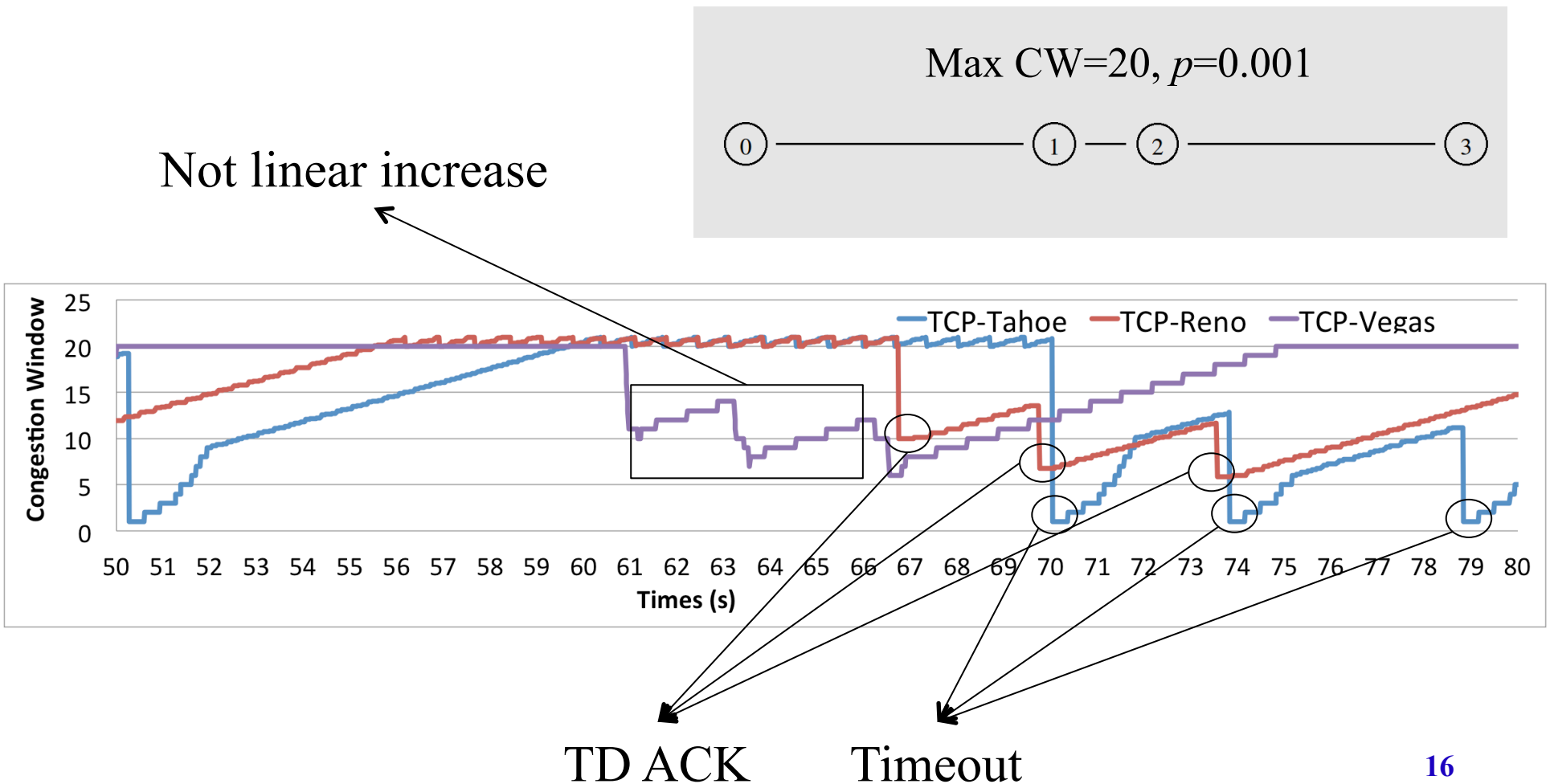
TCP Congestion Control Review

• TCP variants comparison

	Congestion indications	Congestion reactions
Tahoe	Packet losses	<p>Only TO for congestion indication</p> <p>Reduce window to one & go to SS phase</p>
Reno NewReno SACK	Packet losses	<p>- Time-out: Reduce window to one & go to SS phase</p> <p>- TD ACK: Reduce window by a half & go to CA phase</p>
Vegas	Packet losses & RTT delays	<p>Time-out and TD ACK: similar to Reno/NewReno/SACK</p> <p>Keep adjusting RTT delays: $Diff = f(W, RTT)$</p> <p>CA phase</p> <p>- $Diff < \alpha$: $cwnd++$</p> <p>- $Diff > \beta$: $cwnd--$</p> <p>- $\alpha \leq Diff \leq \beta$: $cwnd = cwnd$</p> <p>SS phase</p> <p>- $Diff > \gamma$: go to CA phase</p> <p>Typically, $\gamma = (\alpha + \beta) / 2$; $\alpha = 2$; $2 \leq \beta \leq 4$</p> <div style="background-color: yellow; padding: 5px; margin-top: 10px;"> <p>Expected = $cwnd / BaseRTT$; Actual = $cwnd / RTT$ $Diff = (Expected - Actual) * BaseRTT$</p> </div>

TCP Congestion Control Review

- TCP variants comparison
 - Congestion window trace

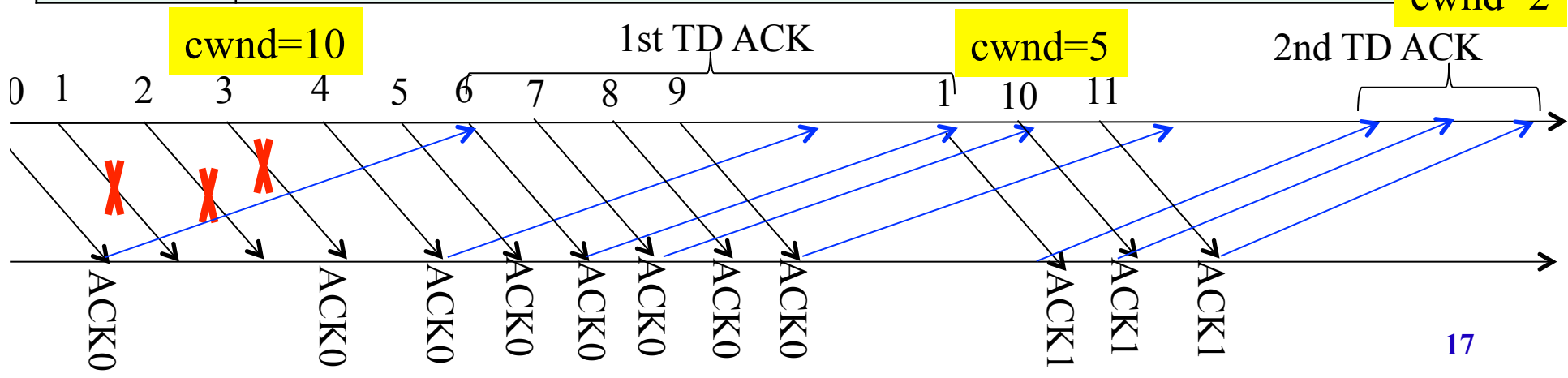


TCP Congestion Control Review

- TCP variants comparison

	Response to multiple packet losses
Reno	Problem with "multiple packet losses in one window" With n packet losses, $cwnd \rightarrow cwnd/2, cwnd/4, \dots, cwnd/(2^n)$ Reducing $cwnd$ multiple times. When $cwnd$ is too small, TO may happen due to the lack of ACKs
NewReno	With n packet losses within a trans window, Reducing $cwnd$ one time
SACK	Reno/NewReno: detection of single lost packet, and re-transmission of one lost packet per RTT SACK (selective acknowledgements): detection of multiple and re-transmission of more than one lost packet per RTT

TO due to the lack of ACKs for pck #3

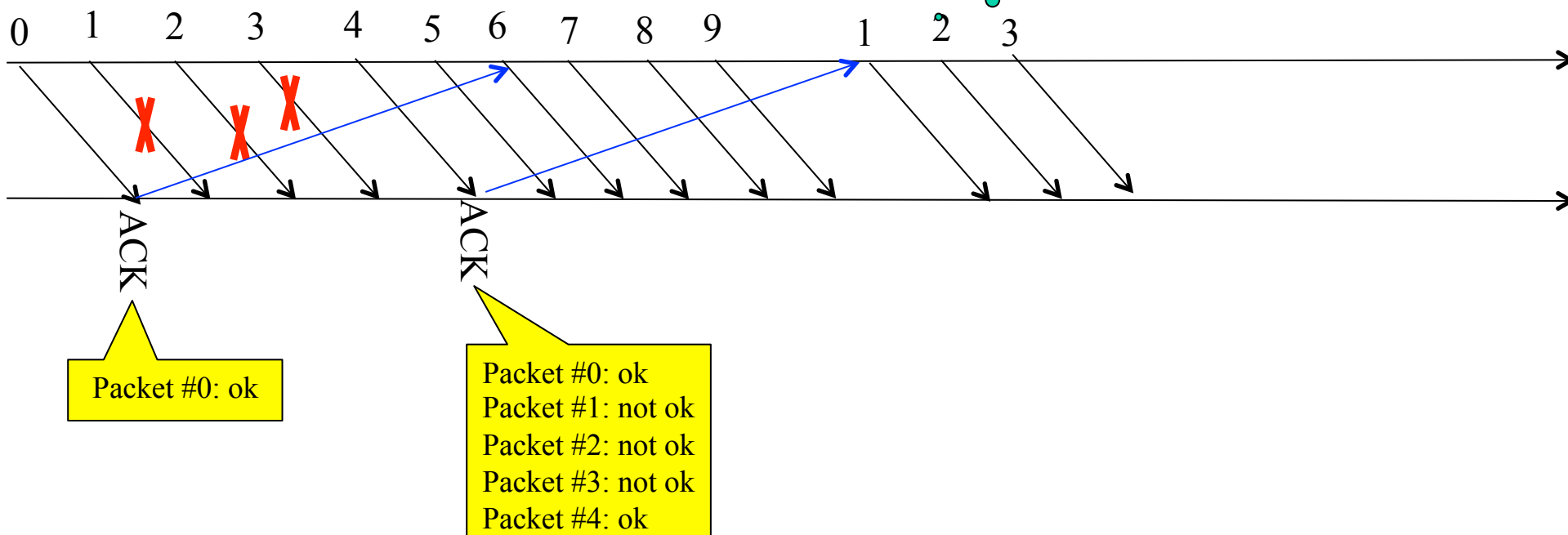


TCP Congestion Control Review

- TCP variants comparison

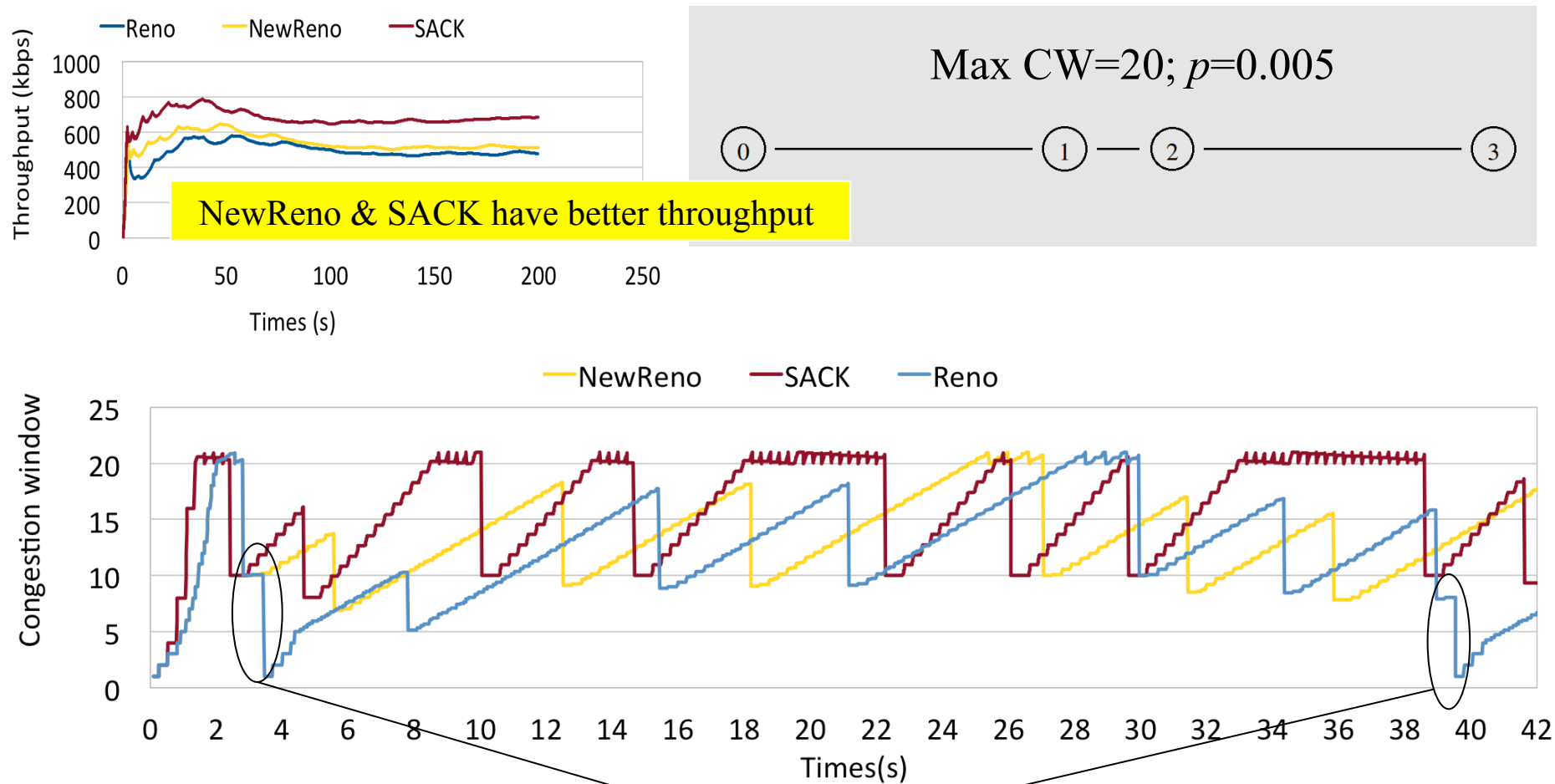
	Response to multiple packet losses
SACK	Reno/NewReno: detection of single lost packet, and re-transmission of one lost packet per RTT SACK: detection of multiple lost packets, and re-transmission of more than one lost packet per RTT

Faster recovery from multiple lose packets event



TCP Congestion Control Review

- TCP variants comparison



Reducing cwnd multiple times, even leading to TO

TCP Modeling

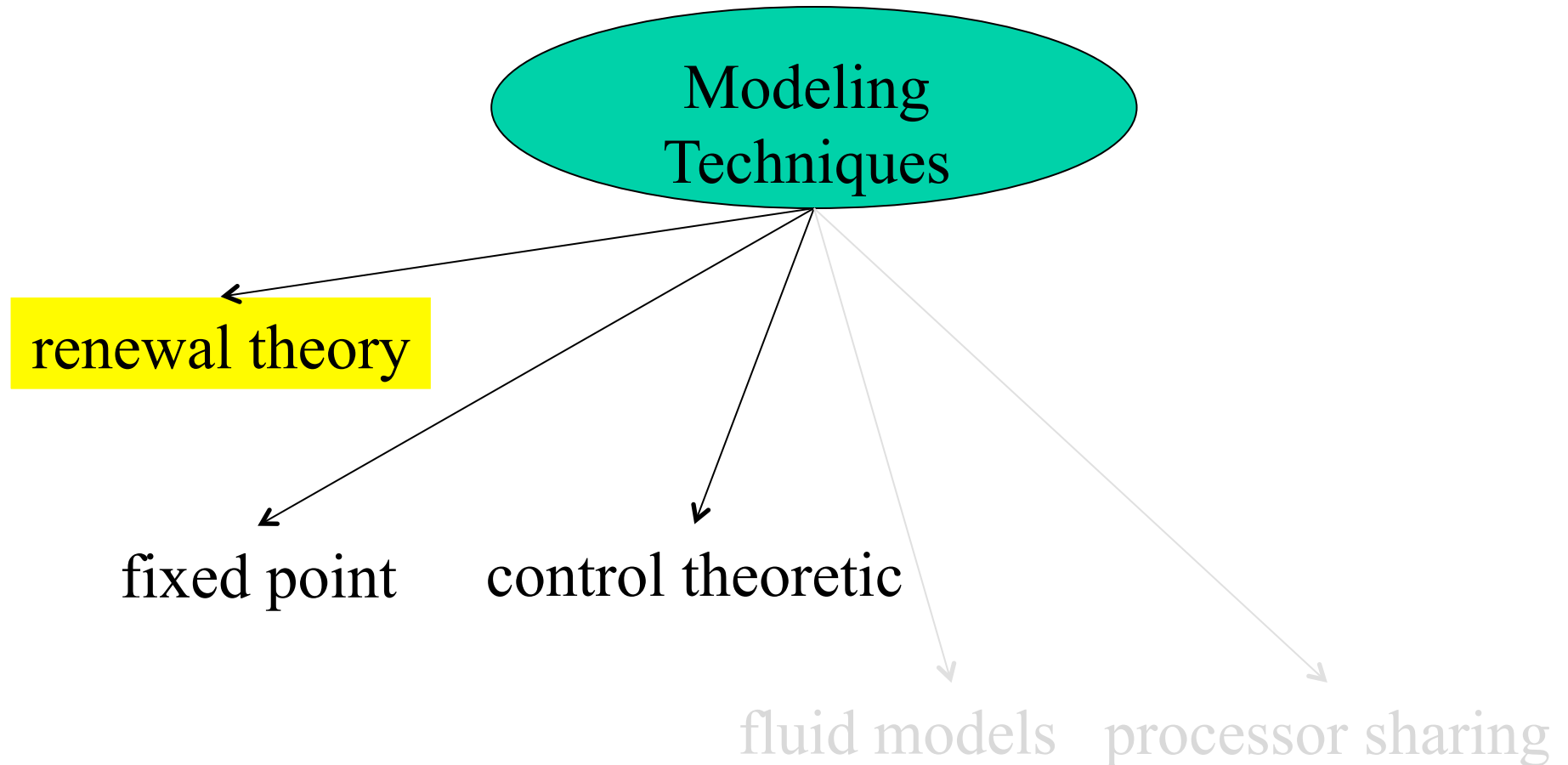
- Objectives

- Understand the fundamental relationship between network parameters and TCP performance

(Throughput, delay,...) <-> (packet loss, round-trip time, topology,...)

- Apply a range of mathematical models to predict TCP performance

TCP Modeling



TCP Modeling: Renewal Theory Models

- Scope
 - study window evolution in terms of cycles
 - Cycle: period between two consecutive loss events
- The steady state TCP throughput

$$Th = \frac{\text{Avg number of packets sent per cycle}}{\text{Avg duration of a cycle}}$$

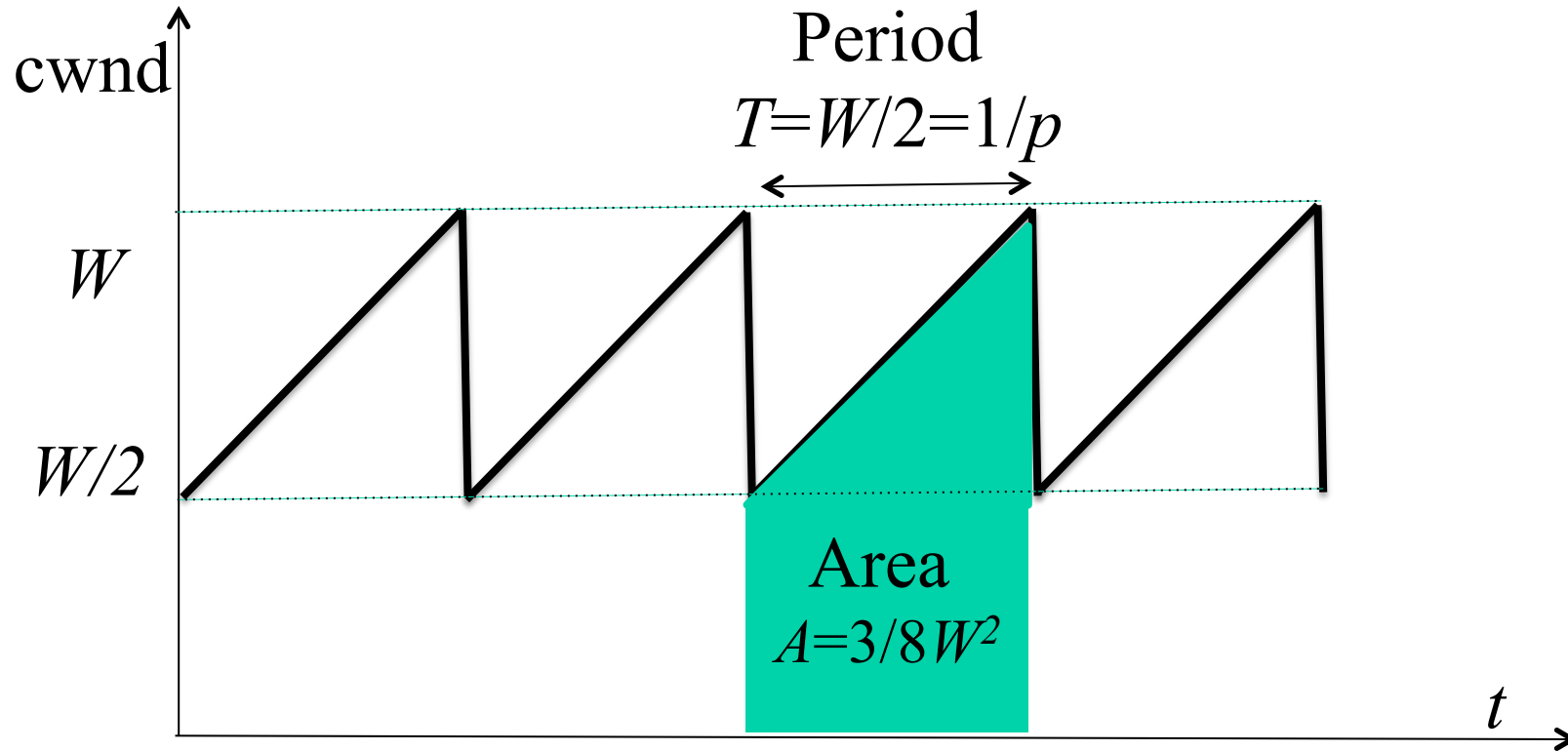
TCP Modeling: Renewal Theory Models

Periodic Model

- The simplest model for TCP throughput
- Assumptions
 - Infinitely long TCP flow
 - Bernoulli losses: packets are lost with a fixed probability p , independently of others
 - Consider periodic TD ACK losses

TCP Modeling: Renewal Theory Models

Periodic Model



$$Th = \frac{A}{L} = \frac{3/8 W^2}{RTT \times W/2} = \frac{1}{RTT \sqrt{(2/3)p}}$$

Qualitatively show:
 throughput is inversely
 proportional to RTT & p

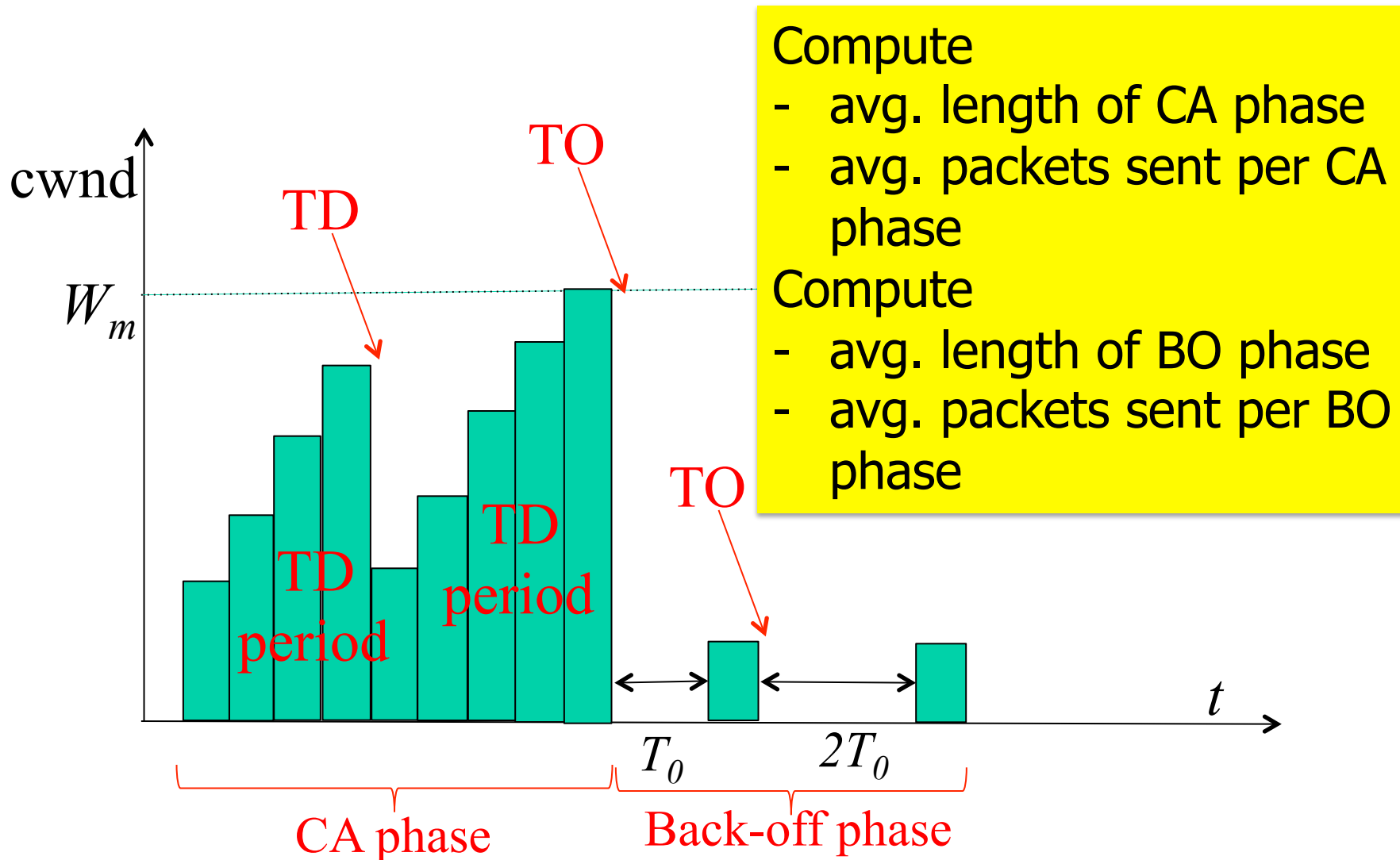
TCP Modeling: Renewal Theory Models

Detailed Packet Loss Model

- Consider
 - Time-out and TD ACK losses
 - Correlated losses: packets are lost with a fixed probability p , independently of others; until first packet lost, remaining window packets are lost
 - Maximum CW (W_m)

TCP Modeling: Renewal Theory Models

Detailed Packet Loss Model



TCP Modeling: Renewal Theory Models

Detailed Packet Loss Model

$$Th = \frac{E[A^{CA}] + E[A^{BO}]}{E[L^{CA}] + E[L^{BO}]} = \frac{E[A^{TD}]E[n^{TD}] + E[A^{BO}]}{E[L^{TD}]E[n^{TD}] + E[L^{BO}]}$$

$$E[.] = f(p, RTT, T_0)$$

Ex:

- The number of TOs in a BO phase has a geometric distribution: $P(R = k) = p^{k-1}(1-p)$

$$\rightarrow E[A^{BO}] = \sum_{k=1}^{\infty} kP(R = k) = 1/p$$

TCP Modeling: Renewal Theory Models

Detailed Packet Loss Model

Ex:

-The duration of a sequence with k TOs is

$$L_k = \begin{cases} (2^k - 1)T_0, & k \leq 6 \\ [63 + 64(k - 6)]T_0, & k > 6 \end{cases}$$

Maximum back-off counter

$$\rightarrow E[L^{BO}] = \sum_{k=1}^{\infty} L_k P(R = k) = T_0 \frac{1 + p + 2p^2 + 4p^3 + 8p^4 + 16p^5 + 32p^6}{1 - p}$$

And so on, see (*) for full derivations

*Jitendra Padhye, Victor Firoiu, Don Towsley, and Jim Kurose.

Modeling TCP throughput: a simple model and its empirical validation.

TCP Modeling: Renewal Theory Models

Detailed Packet Loss Model

$$Th \approx \min \left(\frac{W_m}{RTT}, \frac{1}{RTT \sqrt{\frac{2p}{3}} + T_0 \min(1, 3\sqrt{\frac{3p}{8}}) p(1 - 32p^2)} \right)$$

The diagram illustrates the mapping of terms in the equation to network parameters:

- $\frac{W_m}{RTT}$ is associated with **Maximum CW**.
- $RTT \sqrt{\frac{2p}{3}}$ is associated with **TD losses**.
- $T_0 \min(1, 3\sqrt{\frac{3p}{8}}) p(1 - 32p^2)$ is associated with **Time-out**.

TCP Modeling: Renewal Theory Models

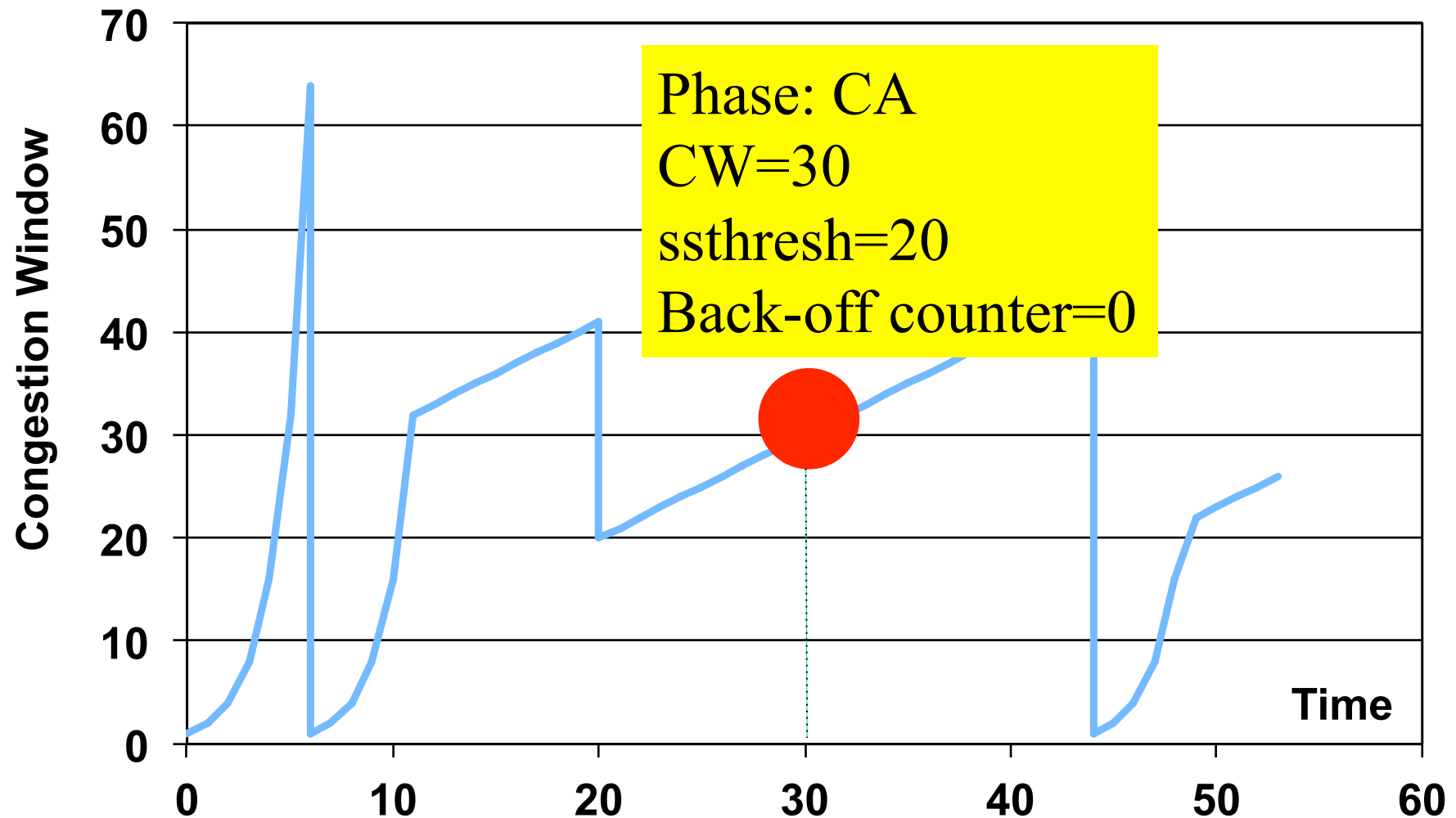
Markov Chain Model

- Chain keeps track of TCP operation through
 - Phases: CA, SS, BO, TO
 - Parameters, e.g., window size, ssthresh and back-off counter.
- Allows more “careful” models

TCP Modeling: Renewal Theory Models

Markov Chain Model

- Observe TCP operation at a cycle & capture its status

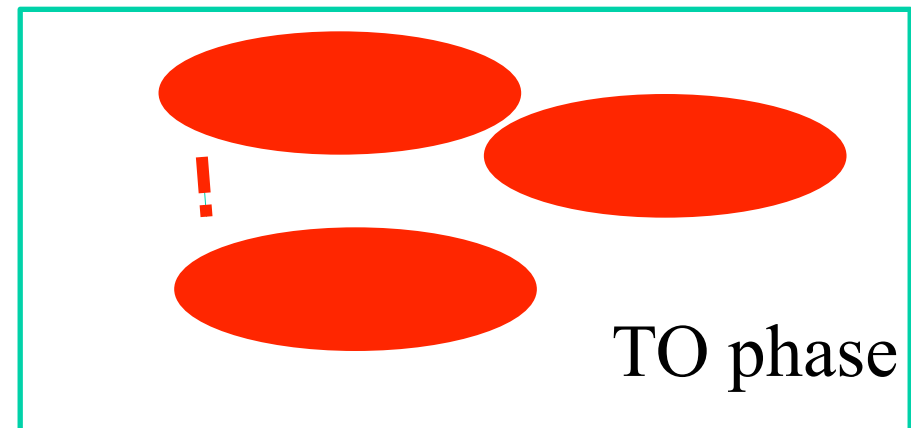
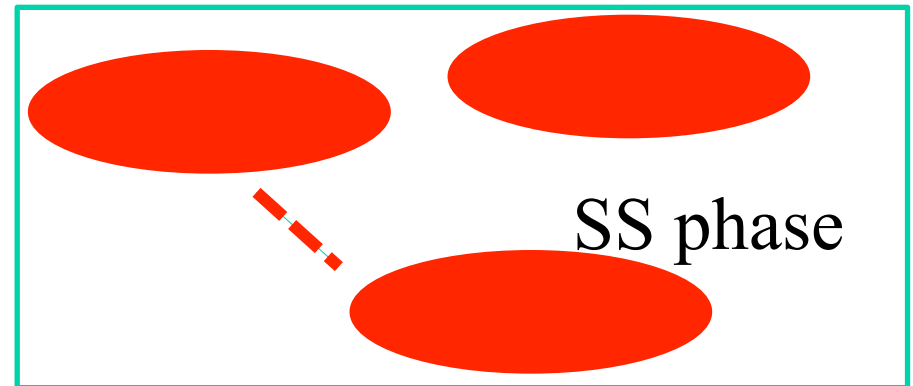
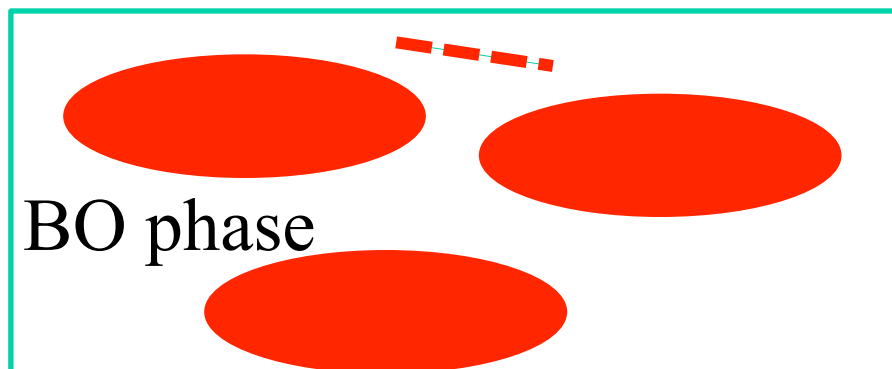
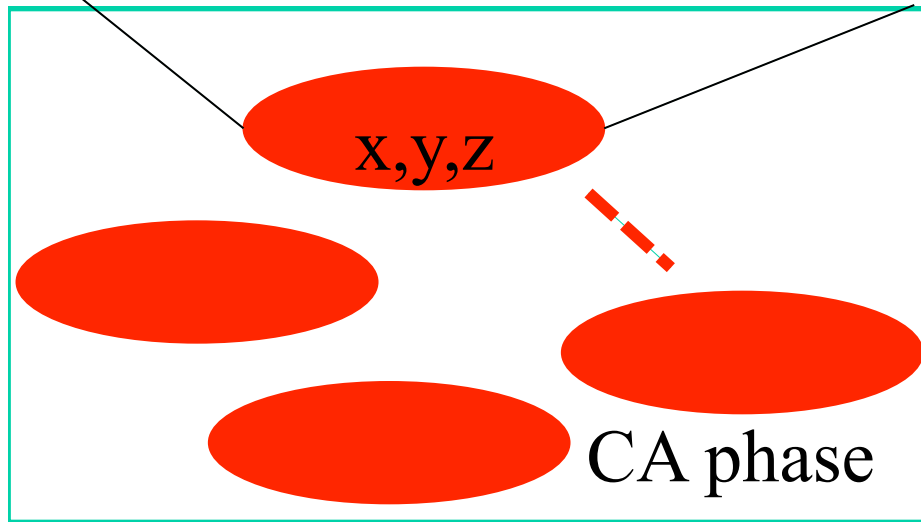


TCP Modeling: Renewal Theory Models

Markov Chain Model

- State space

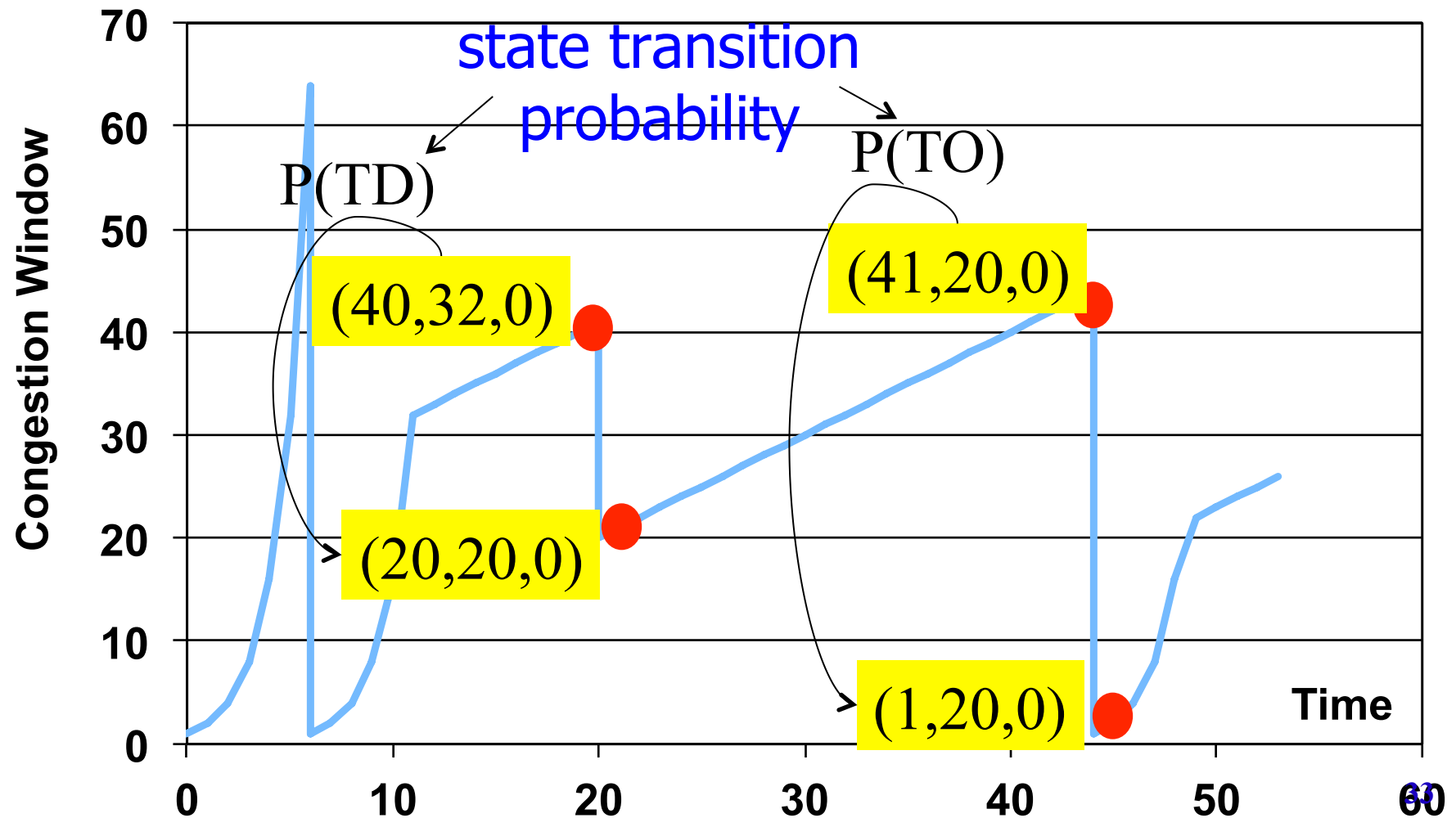
(window size, ssthresh, back-off counter)



TCP Modeling: Renewal Theory Models

Markov Chain Model

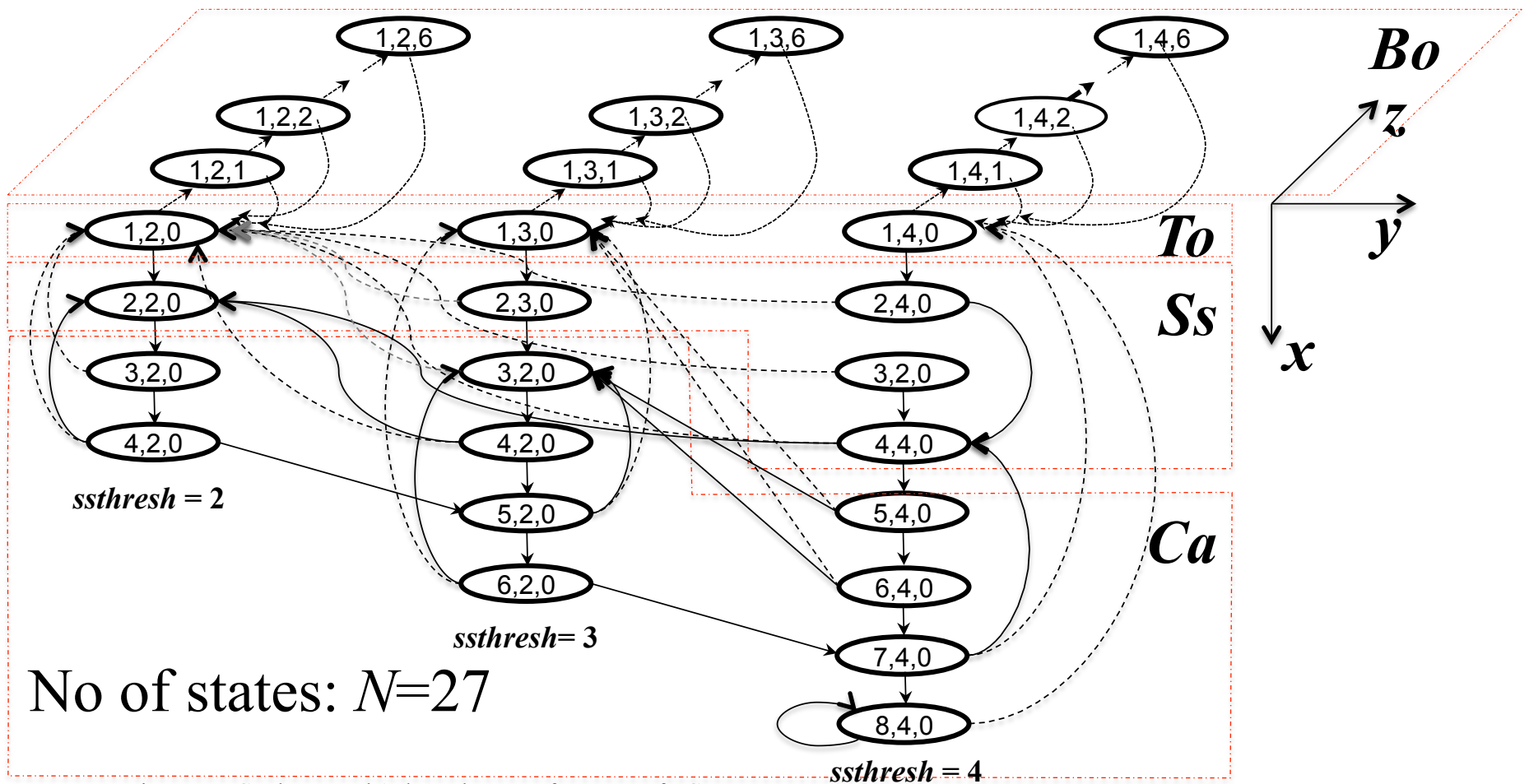
- State connection



TCP Modeling: Renewal Theory Models

Markov Chain Model

- An example of Markov chain for $W_m=8$, $\text{Max_BO}=6$



TCP Modeling: Renewal Theory Models

Markov Chain Model

- Mathematical expression
 - Let $P=[p_1 \ p_2 \ \dots \ p_N]$ be the matrix of steady-state probabilities, where p_i is the probability of the i -th state in the equilibrium
 - Let $Q=[q_{ij}]$ be the transition matrix of the Markov chain with an element q_{ij} being the transition probability from the state i to the state j
 - $q_{ij}=f(\text{packet loss}, CW, \text{phase})$: pre-calculated

TCP Modeling: Renewal Theory Models

Markov Chain Model

- Mathematical expression

$q_{ij} = f(\text{packet loss}, CW, \text{phase}): \text{pre-calculated}$

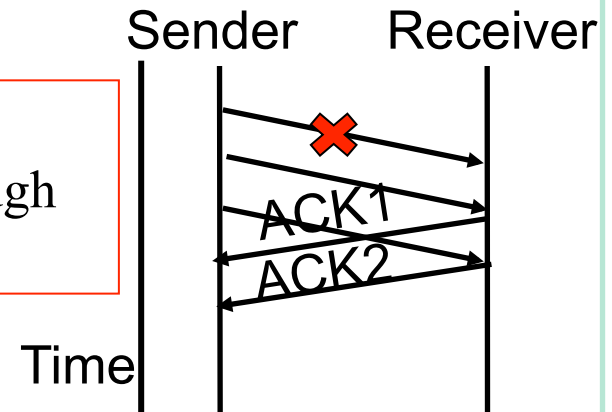
$$P_{TD} \approx \begin{cases} P_W(1) + P_W(2), W \geq 10 \\ P_W(1), 4 \leq W < 10 \\ 0, W < 4 \end{cases}$$

$$P_{TO} \approx \begin{cases} \sum_{i=3}^W P_W(i), W \geq 10 \\ \sum_{i=2}^W P_W(i), 4 \leq W < 10 \\ 1 - P_W(0), W < 4 \end{cases}$$

Prob of i losses from W :

$$P_W(i) = \binom{W}{i} p^i (1-p)^{W-i}$$

Ex: $W=3$
Not enough
3 ACKs



TCP Modeling: Renewal Theory Models

Markov Chain Model

- Mathematical expression

$$\left\{ \begin{array}{l} P = Q \times P \rightarrow \text{the global balance equations} \\ \sum_{i=1}^N p_i = 1 \rightarrow \text{the normalization condition} \end{array} \right.$$

– Solve the set of Eqs by

- Using Matlab to calculate Matrix equations
- (or) Jacobi, Gauss-Seidel

- Having $[p_1 \ p_2 \ \dots \ p_N]$, calculate throughput

$$Th = \frac{\sum p_i CW_i}{\sum p_i RTT_i}$$

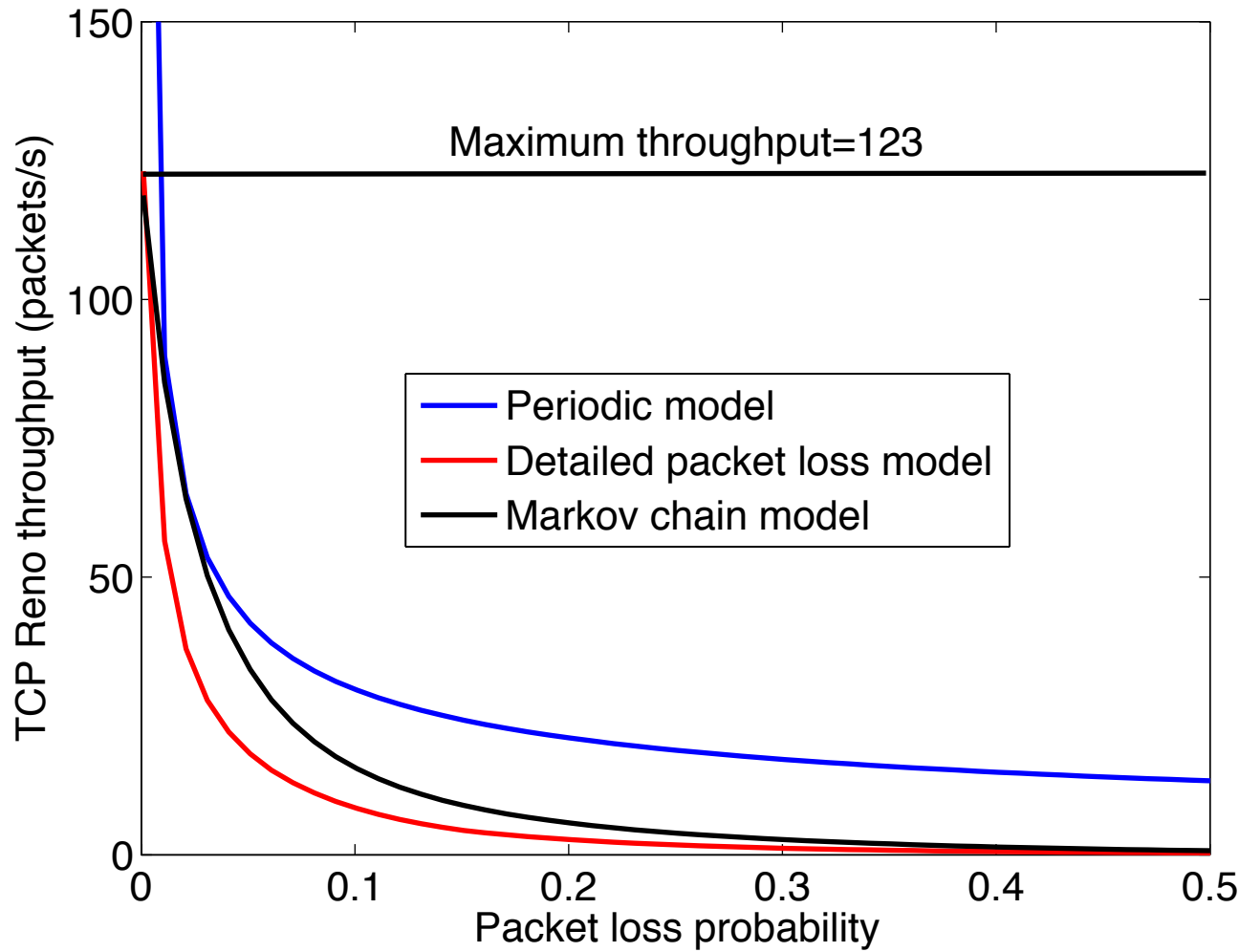
TCP Modeling: Renewal Theory Models

- Comparisons

- Periodic Model/Detailed Packet Loss Model: closed form expressions
- Markov chain:
 - exact form expression, thus having the highest accuracy
 - increasing Max CW significantly increases the state space, thus resulting in high complexity in deriving Markov chain

TCP Modeling: Renewal Theory Models

- Comparisons



$W_m=16$
 $RTT=0.13$ second
 $T_0=5*RTT$

TCP Modeling: Renewal Theory Models

- Advantages

- In most case, throughput is given in closed form
 - Possible to investigate directly how different parameters like pack loss, RTT & Max CW impart throughput

- Disadvantages

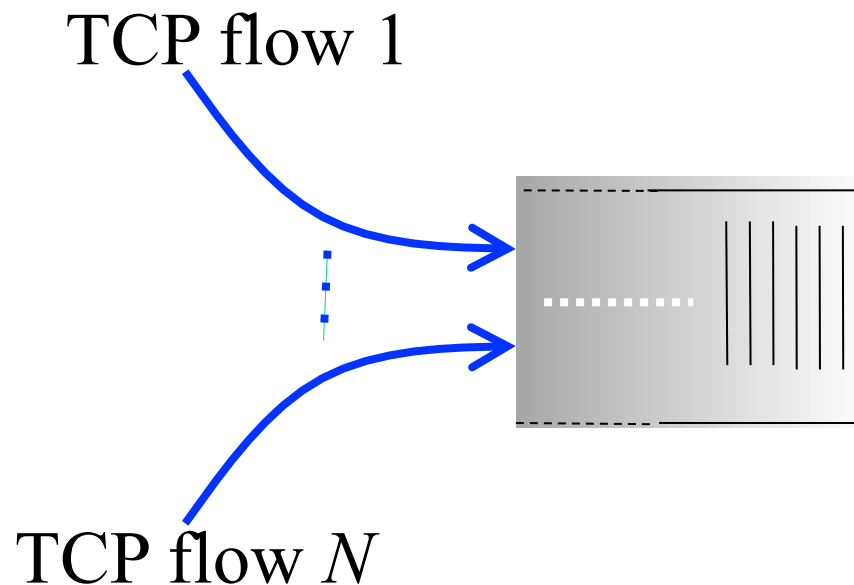
- Primary network parameters like topology & traffic are not taken into account
- Consider for only one single TCP flow
- “Single session & black-box network”

TCP Modeling: Fixed-point Methods

- Scope
 - Modeling of multiple TCP flows in arbitrary network
 - Combining TCP & network models into a framework for TCP-network modeling
- “Multiple sessions & network-aware”

TCP Modeling: Fixed-point Methods

- Consider the simplest scenario
 - N flows going through a bottleneck router
 - Objective: TCP performance & queue performance



TCP Modeling: Fixed-point Methods

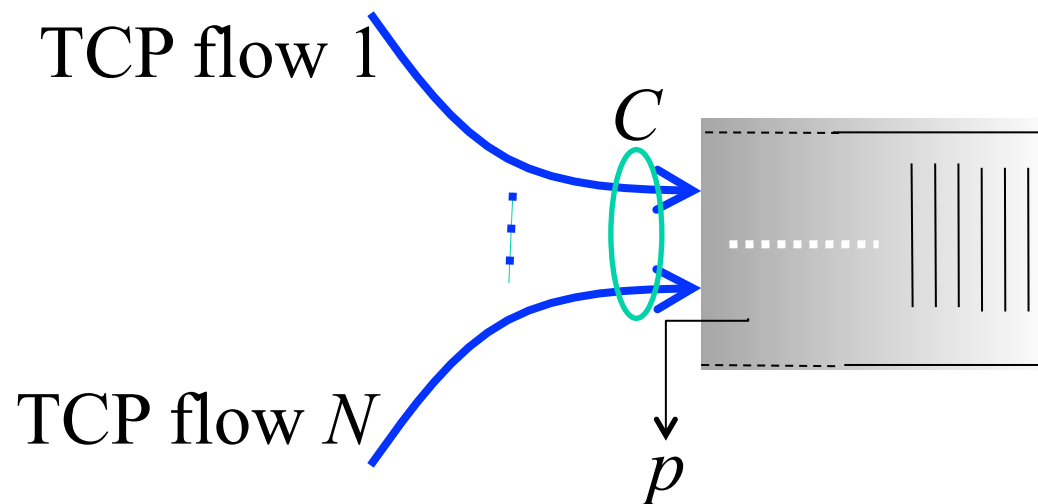
- Approach

- View from queue

- Arrival traffic: aggregated TCP traffics (C)
- Packet loss: blocking pro (p) due to the limited buffer

- View from TCP sources

- All flows see same loss probability, p
- TCP traffic rates (*throughput*) = $Th(p, RTT)$



TCP Modeling: Fixed-point Methods

- Approach

- Solve a *fixed point* problem for p

$$\left\{ \begin{array}{l} \sum_{i=1}^N Th_i(p, RTT_i) = C \\ p = Queue_loss(C) \\ RTT_i = Propagation_delay_i + Queue_delay(C) \end{array} \right.$$

Diagram illustrating the fixed-point problem for p . The equations are grouped by a large left curly brace. Arrows point from the circled terms to their respective modeling components:

- An arrow from $Th_i(p, RTT_i)$ points to "TCP source modeling".
- An arrow from $Queue_loss(C)$ points to "Queue modeling".
- An arrow from $Queue_delay(C)$ points to "Queue modeling".

- Having p , calculate

- TCP performance: $Th(.)$
- Queue performance: $Queue_loss(.), Queue_delay(.)$

TCP Modeling: Fixed-point Methods

- Related studies

- Different TCP source modeling:

- Periodic model, detailed packet loss model, Markov chain model (renewal theory models)

- Different queue modeling:

- M/M/1/B, M/D/1/B

- Extended network topology: multiple routers

TCP Modeling: Fixed-point Methods

- Advantages

- Well combine examined models for TCP sources and for network
- Possible take into account critical network characteristics: topology, no. of flows

- Disadvantages

- Numerical methods used to find the fixed-point in some frameworks require a great deal of implementation work. Ex: multiple routers -> need find a multi-dimensional fixed point

TCP Modeling: Control Theoretic Models

- Motivations

- View from queue

- So far, consider **passive queue management**

- Packet drop event may cause senders to back-off

- No early congestion warning

- Possibly play an active role in controlling TCP connection by **active queue management (AQM)**

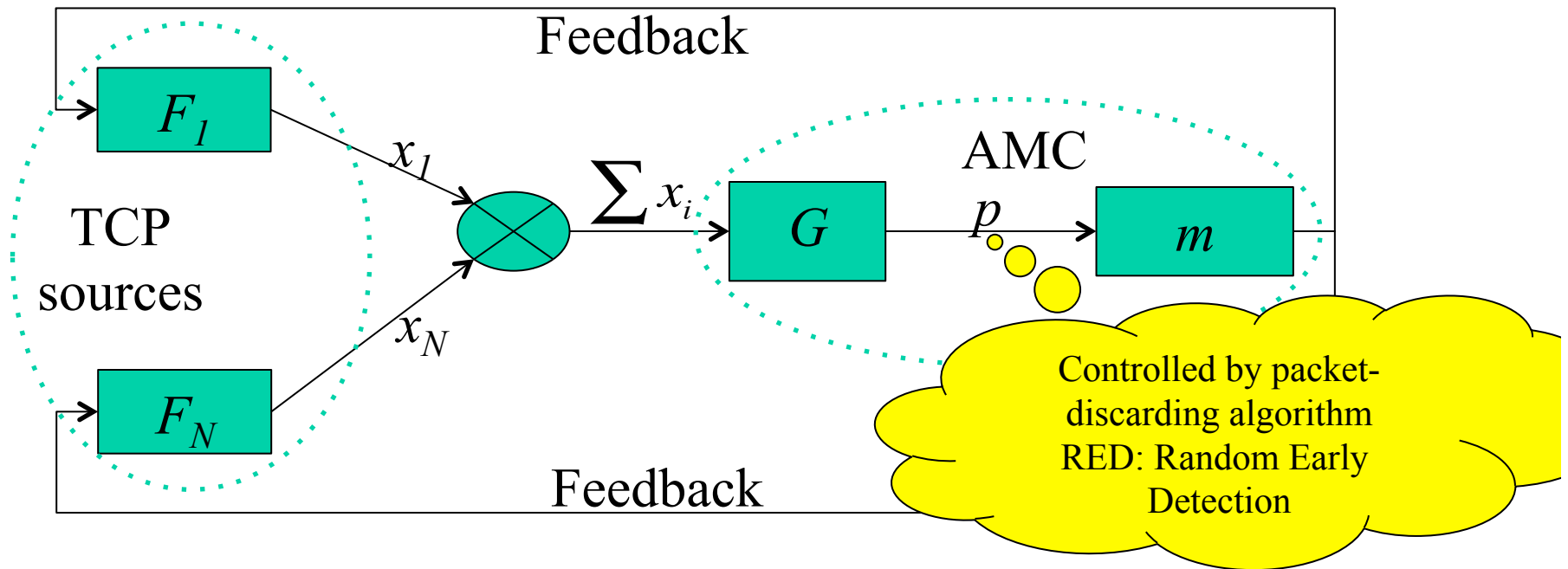
- Perform **preventive random packet drop** before the buffer is full

- Provide a **feedback mechanism** to notify senders of the onset of congestion

- TCP/AQM modeling

TCP Modeling: Control Theoretic Models

- A model of control theory approach



Network congestion signal: $m(p)$

Price (sending cost): p (loss rate, delay, etc.)

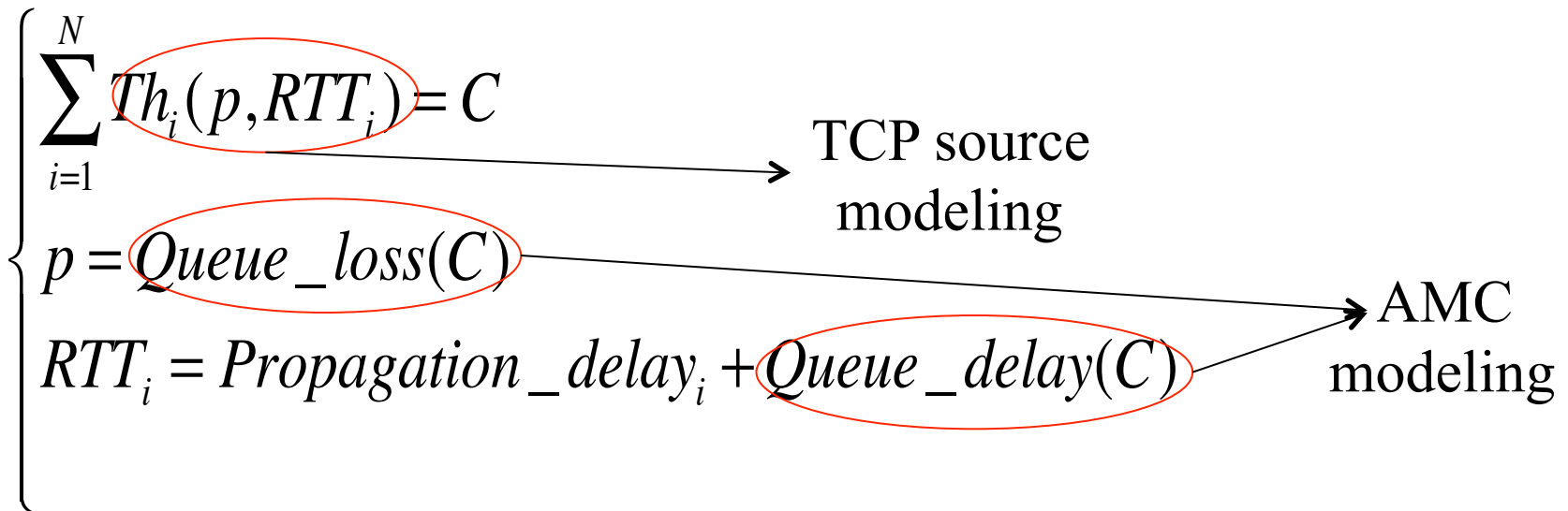
TCP sending rate update rule: $x_s(t+1) = F_s(x_s(t), m(p(t)))$

AMC price update rule: $p(t+1) = G(\sum x_s(t), p(t))$

TCP Modeling: Control Theoretic Models

- Approach

- Can reuse fixed-point methods







- Combine with network optimization

- Maximizing the different betw utilization and sending cost
- > Design AMC operation (RED algorithm)

TCP Modeling: Control Theoretic Models

- **Advantages**
 - More insight interactions betw TCP sources & network
 - Possibly optimize TCP/AQM operations
- **Disadvantages**
 - Require feedback
 - Cost of increased complexity

TCP Modeling: TCP Modeling Comparisons

	Advantages & Disadvantages	Performance analysis	Protocol design
Renewal theory	<ul style="list-style-type: none">- Single session & black-box network- Simple, most popular		
Fixed-point	<ul style="list-style-type: none">- Multiple sessions & network-aware- Complex numerical analysis		
Control theoretic	<ul style="list-style-type: none">- Multiple sessions & network-aware & network optimization- Require feedback- Cost of increased complexity		

Summary

- Review TCP

- Congestion control

- Time-out, TD ACK, Delay RTT
 - SS, CA, TO, BO

- TCP variants

- Tahoe, Reno, NewReno, SACK, Vegas

- Survey TCP modeling

- *Renewal theory*

- Simple, detailed packet loss & Markov chain models

- Fixed-point

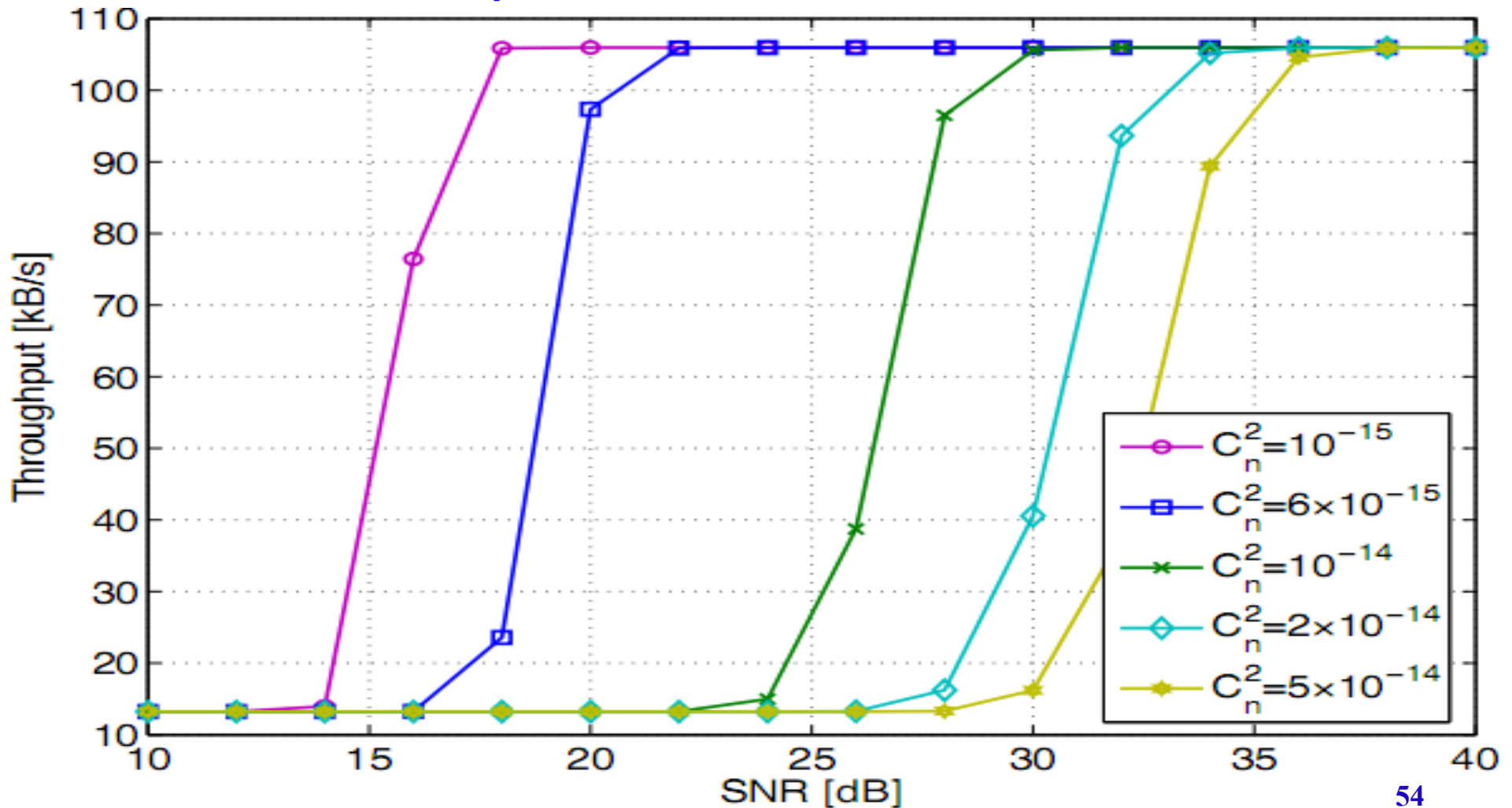
- Control theoretic

Recommended References

Short list	Contents
[1] M. Hassan and R. Jain. High Performance TCP/IP Networking: Concepts, Issues, and Solutions. Book 2003.	Review: TCP/IP fundamentals Review: Performance study of TCP/IP (measurement, simulation, modeling)
[2] Jitendra Padhye, Victor Firoiu, Don Towsley, and Jim Kurose. Modeling TCP throughput: a simple model and its empirical validation. SIGCOM 1998.	Renewal theory: detailed packet loss model
[3] Vuong V. Mai, Truong C. Thang, and Anh T. Pham. Performance of TCP Over Free-Space Optical Atmospheric Turbulence Channels. JOCN 2013.	Renewal theory: Markov chain model Renewal theory: Matlab codes https://drive.google.com/folderview?id=0B1dp1Sn8XivCvEVPSlpRNIBFcW8&usp=sharing
[4] Ols'en, J.. Stochastic Modeling and Simulation of the TCP Protocol. Ph.D thesis 2003.	Survey: TCP modeling (Renewal theory, Fixed-point, Control theoretic)

My Related Studies

Performance of TCP over Free-Space Optical Atmospheric Turbulence Channels



My Related Studies

Throughput Analysis of TCP over Visible Light Communication Indoor Networks

